



Compact Pulsed Hadron Source

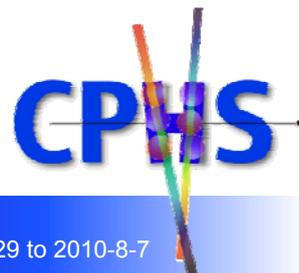
Course G-7

# Introduction to Hadron Synchrotrons

Jie WEI (章傑)

Tsinghua University, Beijing

清华大学 工程物理系 强子应用及技术中心



6<sup>th</sup> OCPA Accelerator School, Beijing, 2010-7-29 to 2010-8-7

## Class Outline (I)

### 1. Overview

- 1.1 History, trends, RCS vs. AR
- 1.2 Low-loss design philosophy

### 2. Accelerator system: design & technical issues

- 2.1 Lattice
- 2.2 Acceptance, emittance, beam scraping & collimation
- 2.3 Injection
- 2.4 Acceleration
- 2.5 Extraction
- 2.6 Magnet system & field error compensation
- 2.7 Vacuum chamber & shielding
- 2.8 Beam diagnostics & machine protection

## *Class Outline (II)*

### 3. Beam dynamics: intensity limiting mechanisms

- 3.1 Transverse tune shifts & resonances
- 3.2 Beam loss mechanisms
- 3.3 Collective effects
- 3.4 Electron cloud effects
- 3.5 Computer simulation codes

### 4. Future applications & developments

References

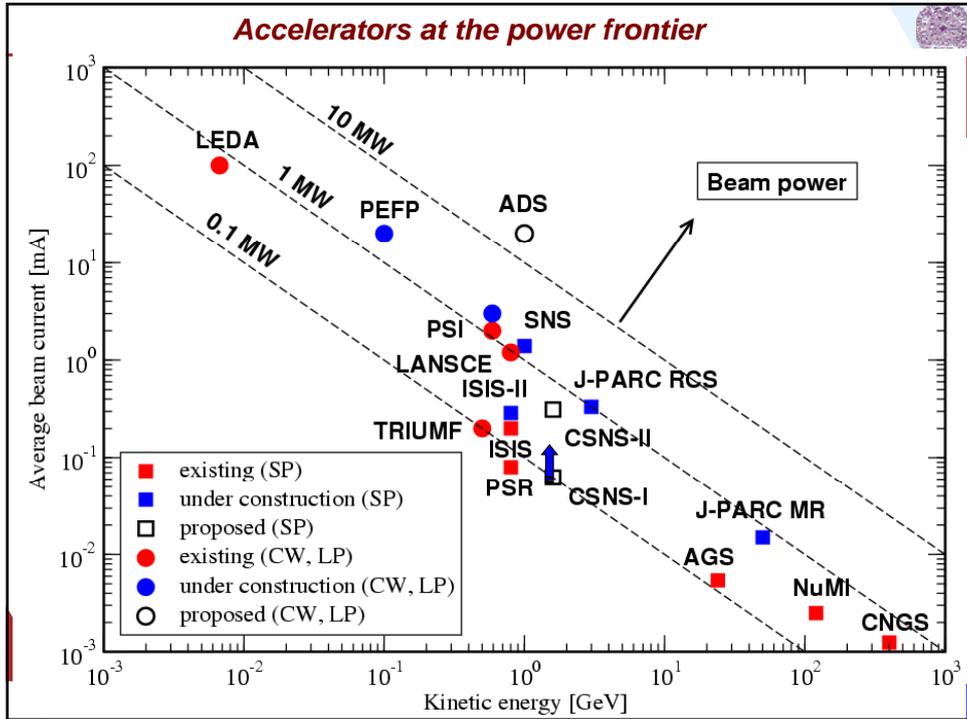
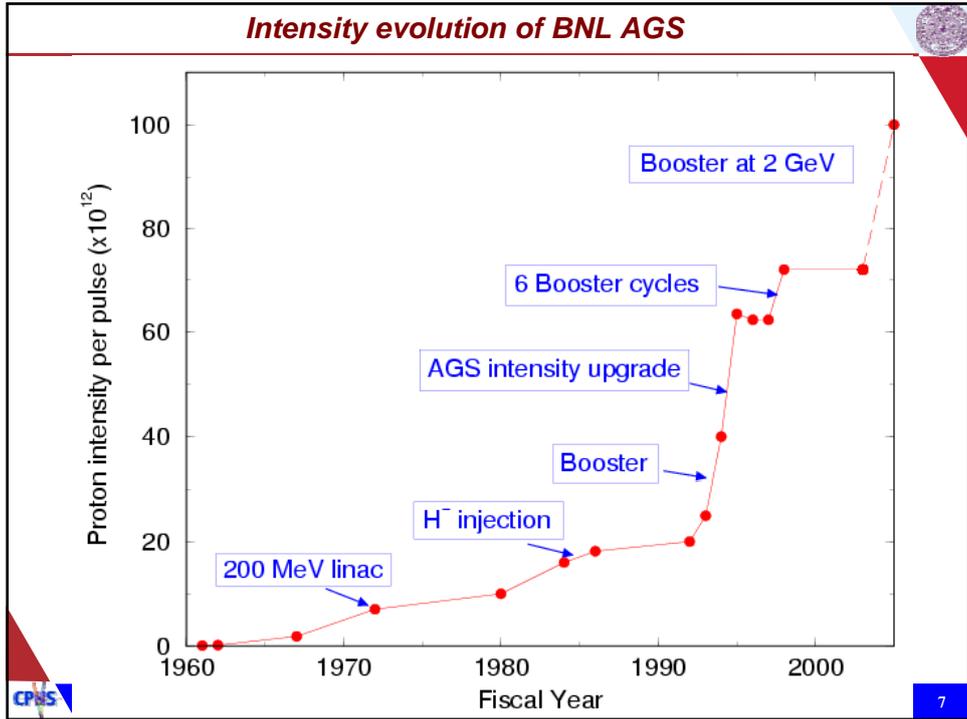
Problems

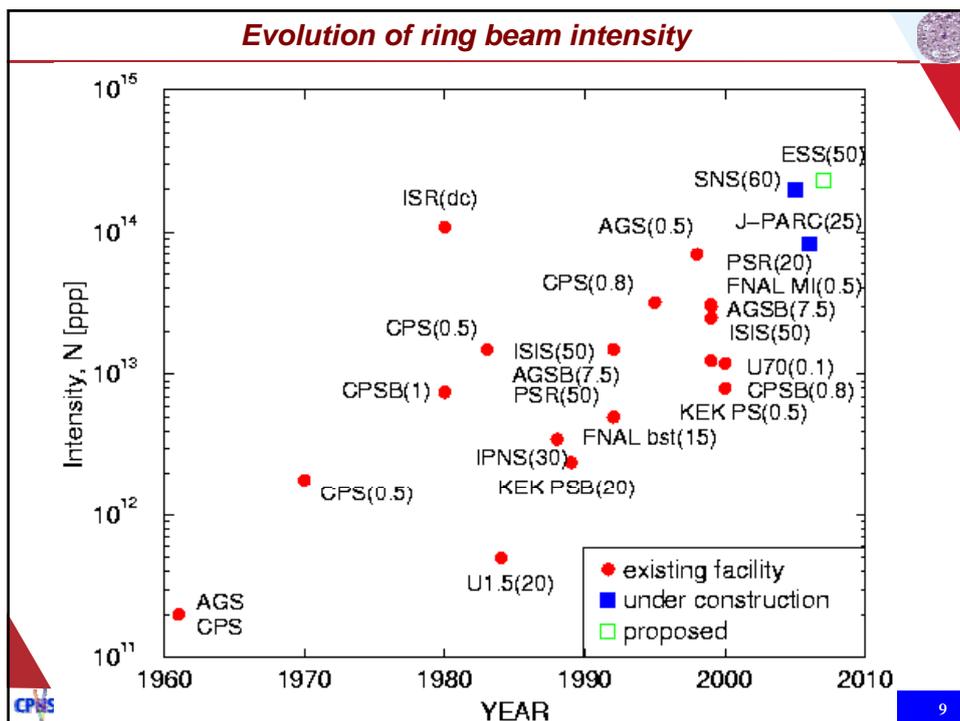
## 1. Overview

## 1.1 History, trends, rapid cycling synchrotron vs. accumulator ring

### *History (what made it possible?)*

- 1945 (E.M. McMillan, V.Veksler):  
**Synchrotron**
- 1950 – 1952 (E.D. Courant, M.S. Livingston, H.S. Snyder, N.C. Christofilos):  
**Alternating-Gradient focusing**
- Development of intense  $H^-$  and  $H^+$  source
- 1970 (I.M. Kapchinskii, V.A. Teplyakov):  
**Radio Frequency Quadrupole**
- Linac development:
  - **Permanent magnet quad for DTL, super-conducting RF, etc.**





### Mega-Watt project examples

	Energy [GeV]	Current [mA]	Rep.-rate [Hz]	Ave. power [MW]	Type
SNS	1	1.5	60	1.4	AR
J-PARC	3	0.33	25	1	RCS
CERN PD	2	2	100	4	AR
RAL PD	5	0.4	25	2	RCS
FNAL PD	16	0.25	15	2	RCS
EA	1	10 -- 20	CW	10 -- 20	cyclotron
APT	1.03	100	CW	103	linac
TRISPAL	0.6	40	CW	24	linac
ADTW	0.6 – 1.2	20 -- 50	CW	> 20	linac
μ-collider driver	30	0.25	15	7.0	RCS

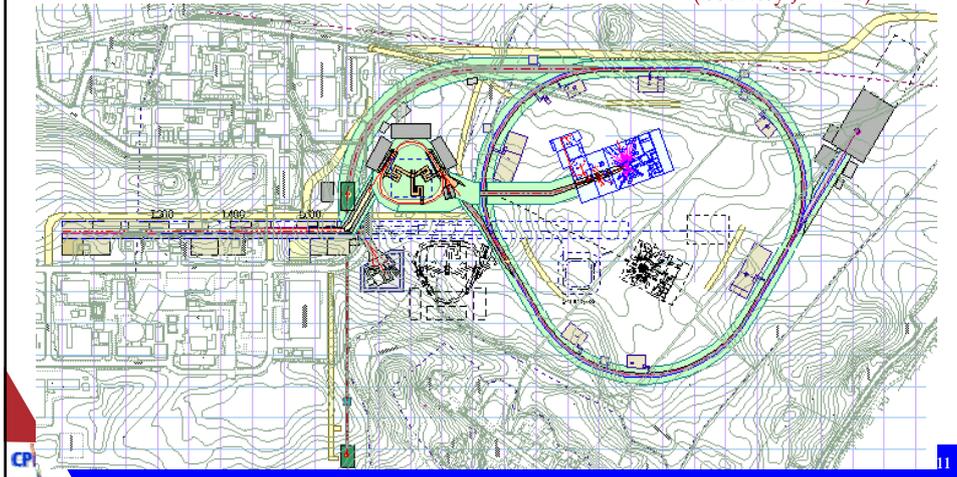
### J-PARC schematic layout

## Japan Proton Accelerator Research Complex

Similar cost, similar schedule (due 2006 ~ 2007)

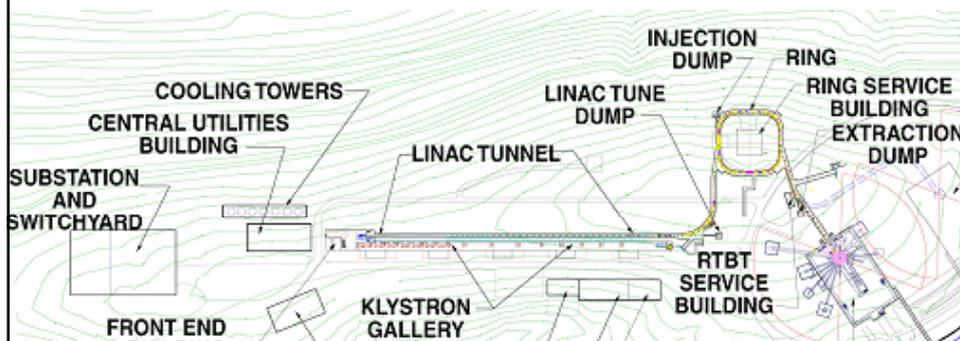
Ring clusters with expandable energy range; multipurpose

(Courtesy J-PARC)



### SNS schematic layout

- Built on top of the ridge, expandable with a 2<sup>nd</sup> target (but wrong location for a long pulse target station)
- Extra long linac tunnel is reserved for future energy/power upgrade; ring capacity reserved



### *Pulsed accelerator options:*

#### ■ Full energy linac & accumulator ring

- Simpler ring design, no magnet ramping, better field quality
- Shorter ring storage time, less instability, lower beam loss
- Not compatible to energy/power upgrade
- Longer, more expensive linac

#### ■ Low energy linac & rapid cycling synchrotron

- Easy on energy/power upgrade with additional RCSs
- Less overall cost for facilities of lower (<1 MW) beam power
- More RF, higher magnet strength for ring
- Difficult to control beam loss

### *SNS ring design debates*

#### ■ Accumulator or rapid-cycling synchrotron?

- Loss-power comparison: PSR loss 0.3%; usual RCS loss ~10%
- RF, power supply, beam-pipe shielding, magnetic & track errors

#### ■ FODO-doublet lattice or all-FODO lattice?

- Long, matched straight section: injection independent of tuning; collimation efficiency from ~ 80% to 95%

#### ■ Do we need sextupoles? Energy corrector & spreaders?

- Four-family chromatic sextupole for tune-spread control & match
- Energy correctors & spreaders for longitudinal painting

#### ■ Can we use permanent magnets? Certainly not for a cold linac!

#### ■ Should the aperture be reduced? No, aperture is everything!

#### ■ Solid-core or laminated-core magnets (\*)?

- Large field variation in a solid-core magnet (although lower cost)

## 1.2 Low-loss design philosophy

### *Low-loss design philosophy*

- **Localize beam loss to shielded area**
  - 2-stage collimation, 3-step beam-gap chopping/cleaning
- **A low-loss design**
  - Proper lattice design with adequate aperture & acceptance  $A/\epsilon > 2$
  - Injection painting; Injection & space-charge optimization  $\Delta Q < 0.2$
  - Resonance minimization; Magnet field compensation & correction
  - Impedance & instability control
- **Flexibility**
  - Adjustable energy, tunes; Flexible injection; Adjustable collimation
  - Foil & spare interchange
- **Engineering reliability**: heat & radiation resistant
- **Accidental prevention**: Immune to front end, linac & kicker fault

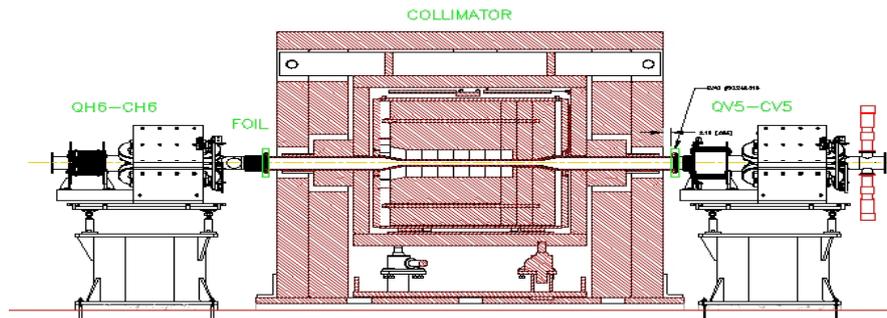
## Secondary collector design

Length enough to stop primary protons ( $\sim 1$  m for 1 GeV beam)

Layered structure (stainless steel particle bed in borated water, stainless steel blocks) to shield the secondary (neutron,  $\gamma$ )

Fixed, enclosing elliptical-shaped wall for operational reliability

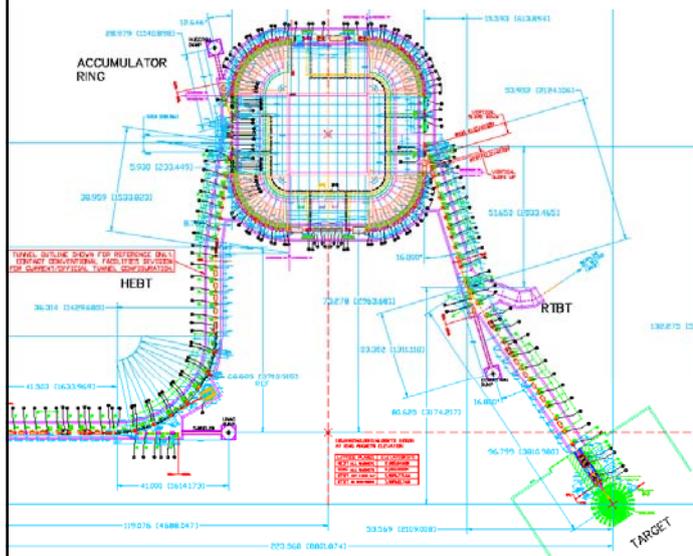
Double-wall Inconel filled with He gas for leak detection



## 2. Accelerator system: design & technical issues

## 2.1 Lattice

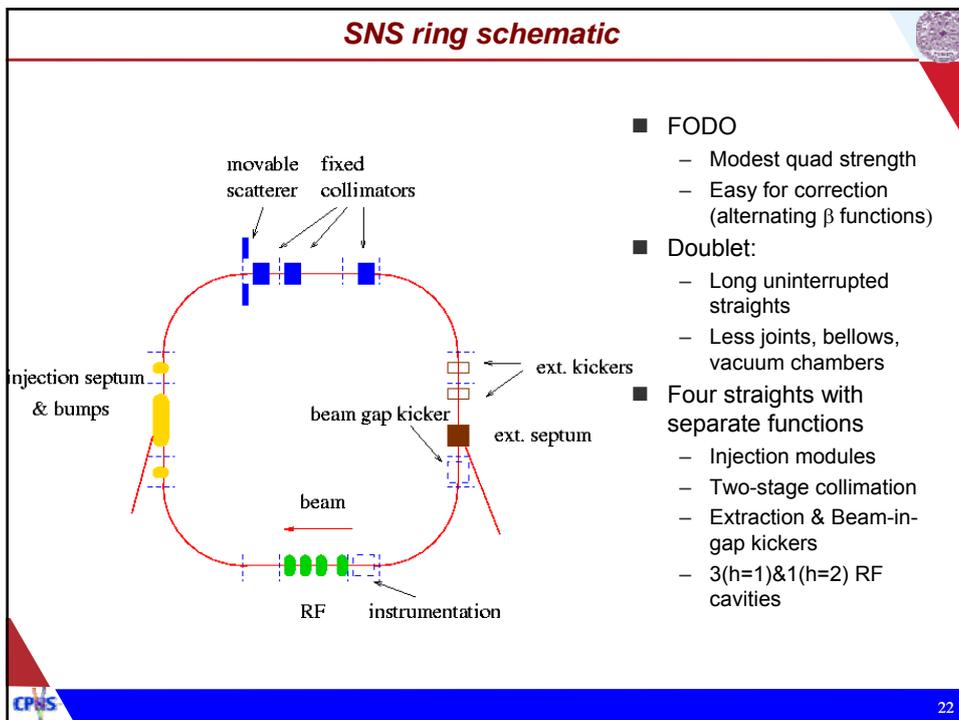
### *Symmetry, resonance, free space*



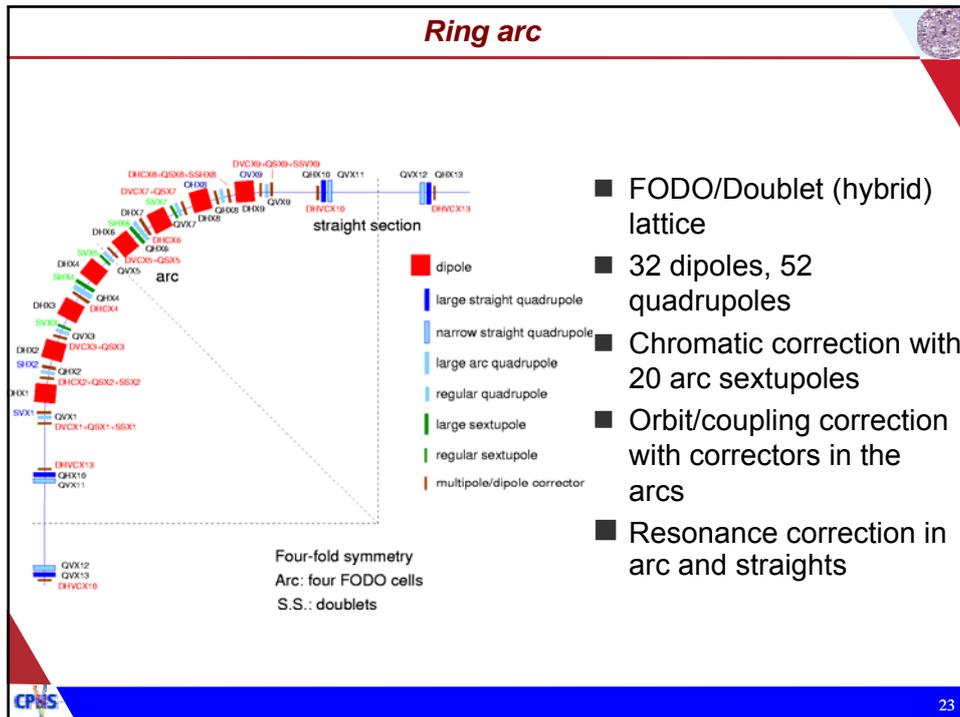
- higher symmetry, fewer structural resonances
- lower symmetry, longer free space

TABLE I. Examples of favorable working points in the transverse tune space for some existing and designed rings for high-intensity operations (Sec. III.A.5).

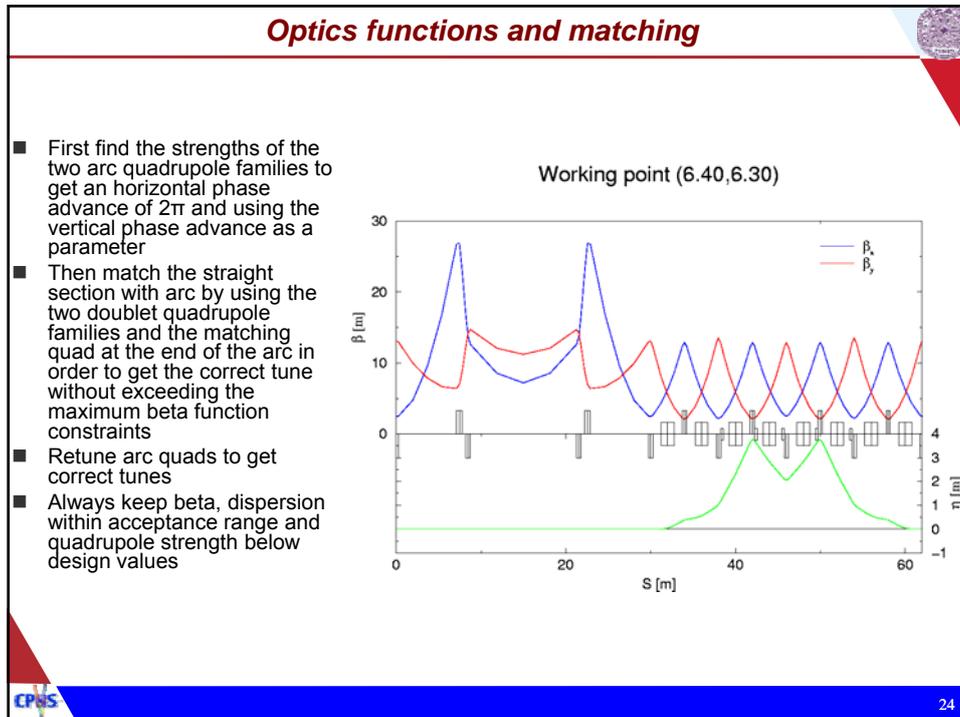
Machine	Superperiodicity	Horizontal tune	Vertical tune	Proton per pulse
<b>Operating:</b>				
AGS	12	8.8	8.9	$7 \times 10^{13}$
AGS Booster	6	4.8	4.9	$2.3 \times 10^{13}$
CERN's PSB	16	4.28	5.56	$1.3 \times 10^{13}$
CERN's PS	10	6.25	6.30	$3.2 \times 10^{13}$
CERN's SPS	6	26.62	26.58	$4.6 \times 10^{13}$
FNAL's Booster	24	6.7	6.8	$5 \times 10^{12}$
FNAL's MI	2	26.425	25.415	$3 \times 10^{13}$
IPNS	6	2.20	2.32	$3.5 \times 10^{12}$
ISIS	10	4.31	3.83	$2.5 \times 10^{13}$
KEK's PSB	8	2.17–2.10	2.30–2.40	$2.4 \times 10^{12}$
KEK's PS	4	7.14–7.16	5.24	$8 \times 10^{12}$
PSR	10	3.19	2.19	$5 \times 10^{13}$
U1.5	12	3.92	3.75	$5 \times 10^{11}$
U70	12	9.92	9.85	$1.2 \times 10^{13}$
<b>Designed:</b>				
ESS	3	4.19	4.31	$2.3 \times 10^{14}$
J-PARC 3-GeV	3	6.72	6.35	$8.3 \times 10^{13}$
J-PARC 50-GeV	3	22.4	22.25	$3.3 \times 10^{14}$
SNS	4	6.23	6.20	$2 \times 10^{14}$



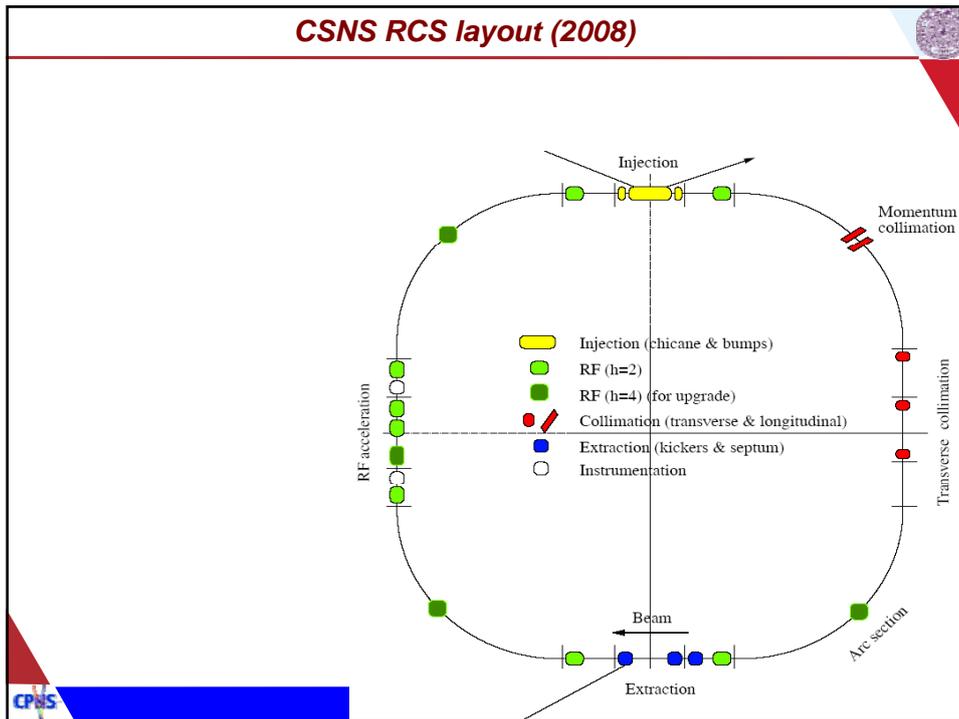
## Ring arc



## Optics functions and matching

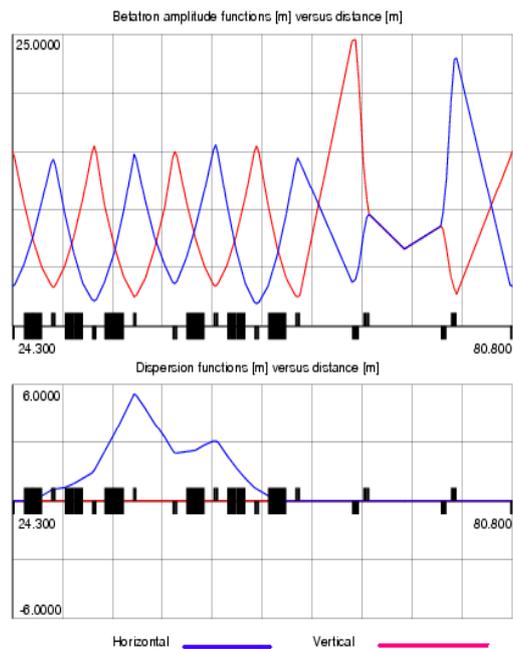


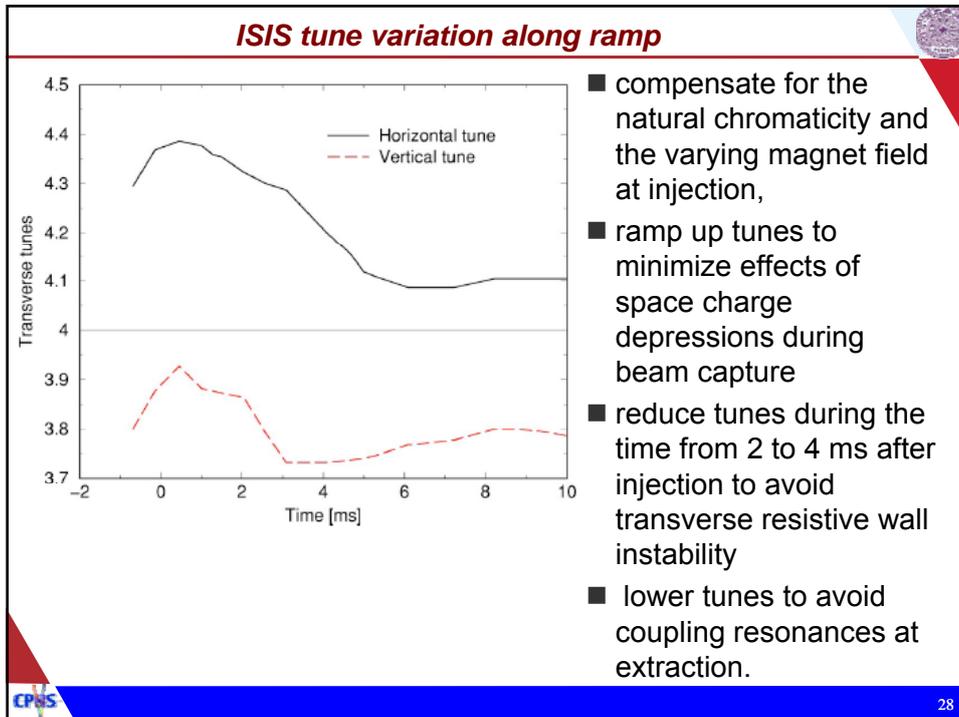
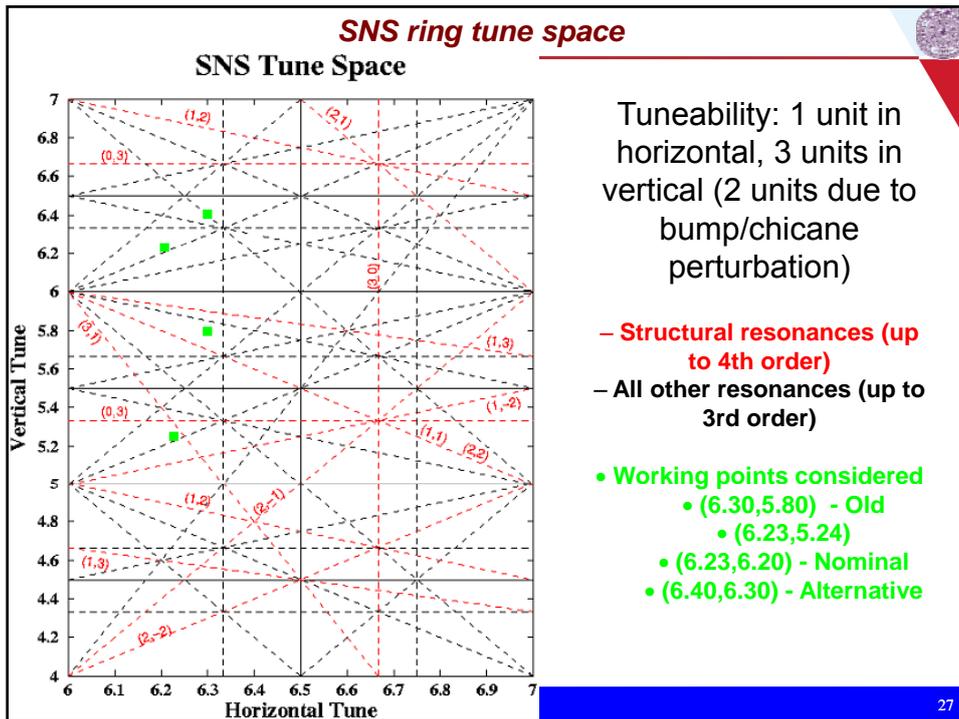
## CSNS RCS layout (2008)



## CSNS RCS lattice (2008)

- Four-fold symmetry
  - Separated functions
- FODO arc (3.5 cell at each arc)
  - Easy correction
- Dispersion-free doublet straight
  - long, uninterrupted straight for collimation & injection
- Missing-gap momentum collimation
  - High momentum cleaning efficiency
- Easy to modify
  - New lattice for longer straight sections





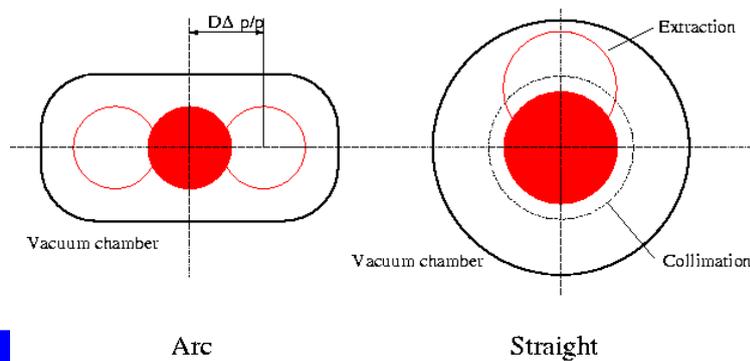
## 2.2 Acceptance, emittance, beam scraping & collimation

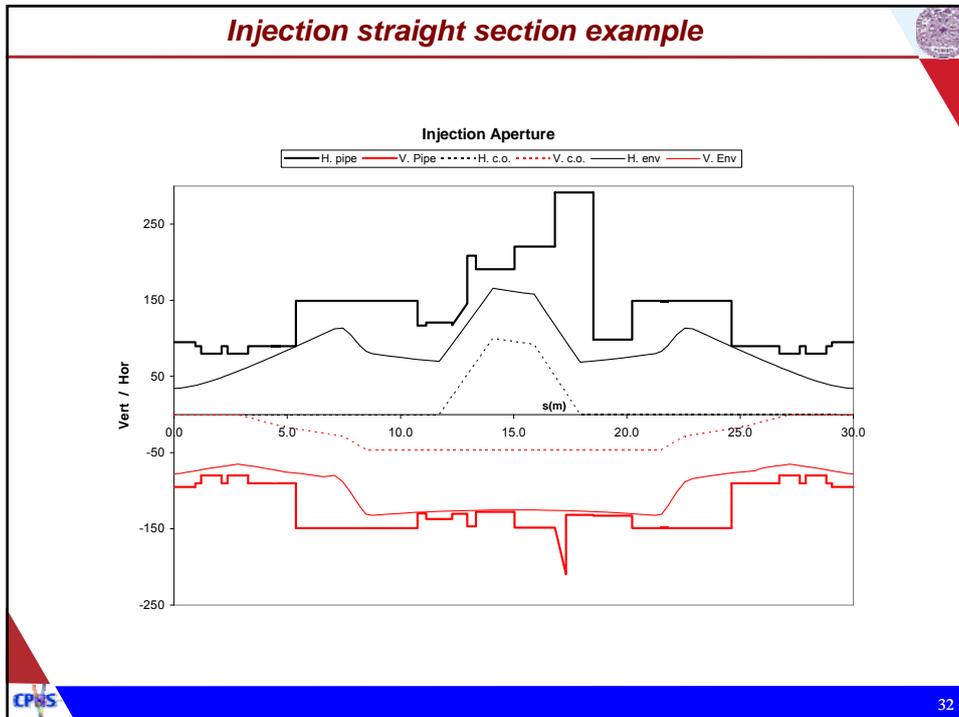
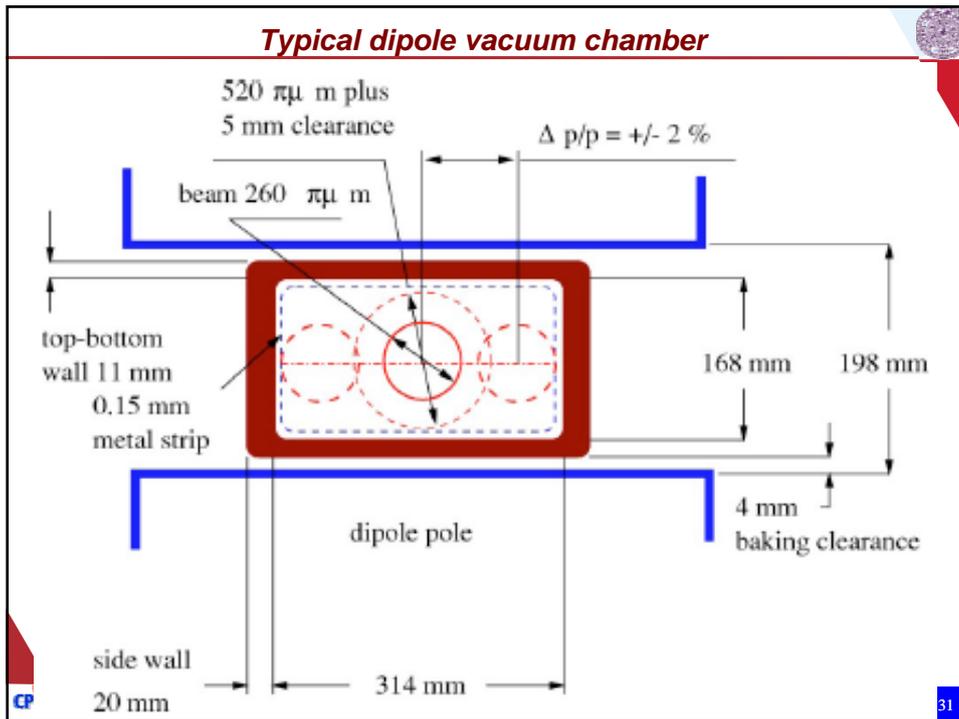
### *Transverse acceptance*

#### ■ Transverse motion

$$x(s) = x_{\beta}(s) + x_p(s) + x_{c,0}(s) + x_c(s)$$

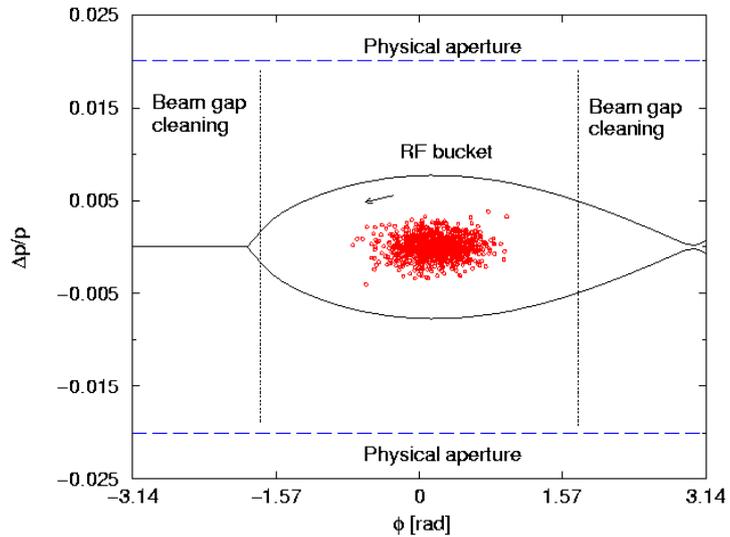
#### ■ Betatron amplitude, off-momentum closed orbit, design closed orbit, closed-orbit deviation



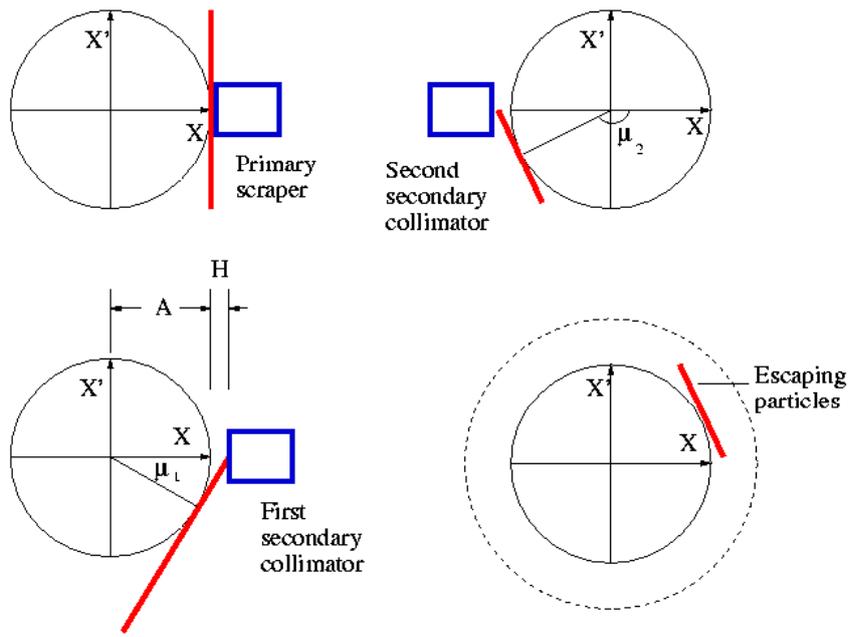


## Longitudinal acceptance

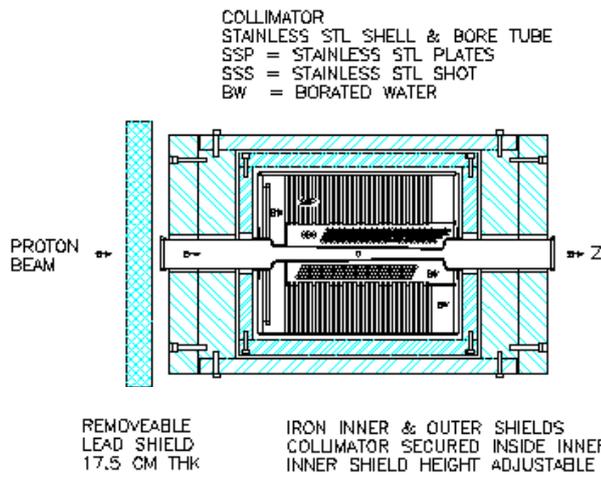
- Momentum acceptance from transverse aperture at high-dispersion region
- RF bucket admittance
- Beam gap reserve



## Collimation optimization



## Collimator design



- Stops primary proton
  - Longer length for higher energy
- Contains secondary particles with layered material
  - Neutron
  - $\gamma$  ray
- Choice of material
  - Vacuum out-gassing
  - Secondary scattering
  - Heat resistance
  - Radiation resistance
  - Stopping capability

courtesy H. Ludewig, N. Catalan-Lasheras

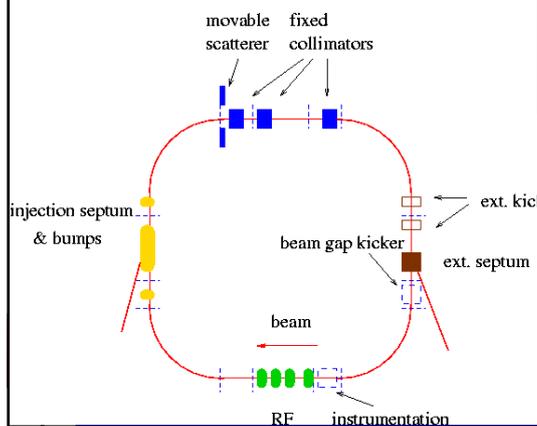
SCHEMATIC OF COLLIMATOR COMPONENTS  
 HORIZONTAL SECTION

35

## Ring scraper & collimator

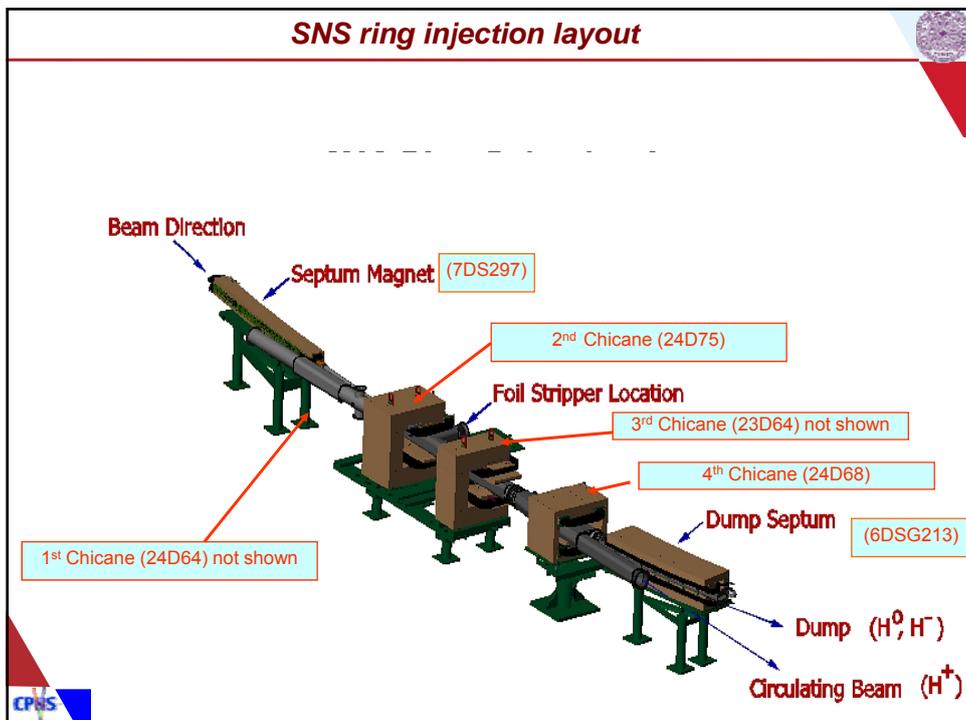
4 scrapers spaced at 45 degree angle  
 3 collimators; first one to shield scraper shine

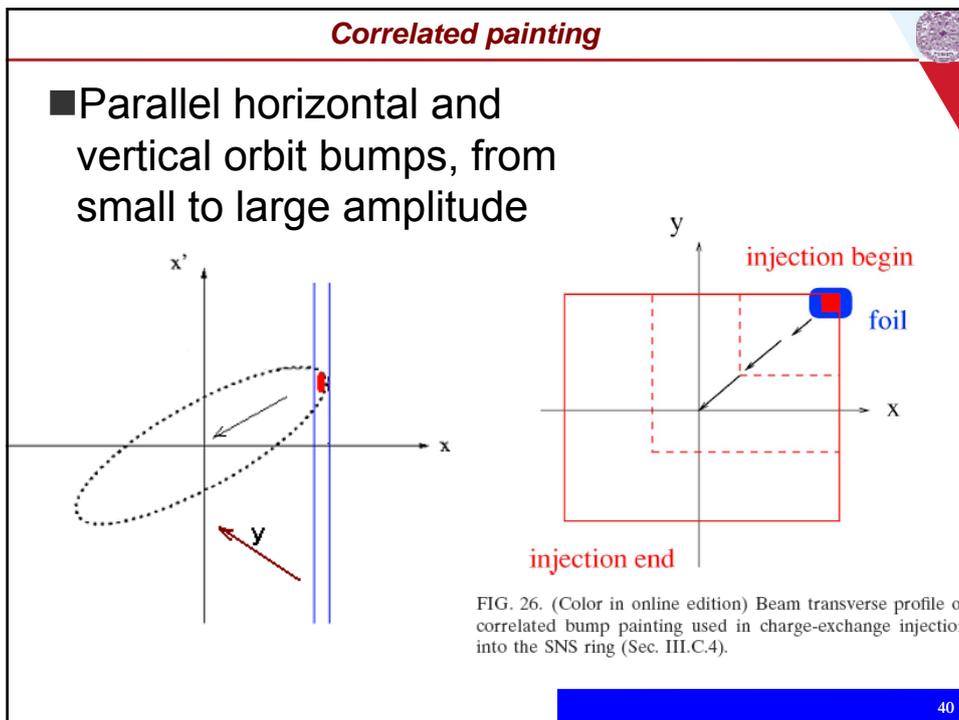
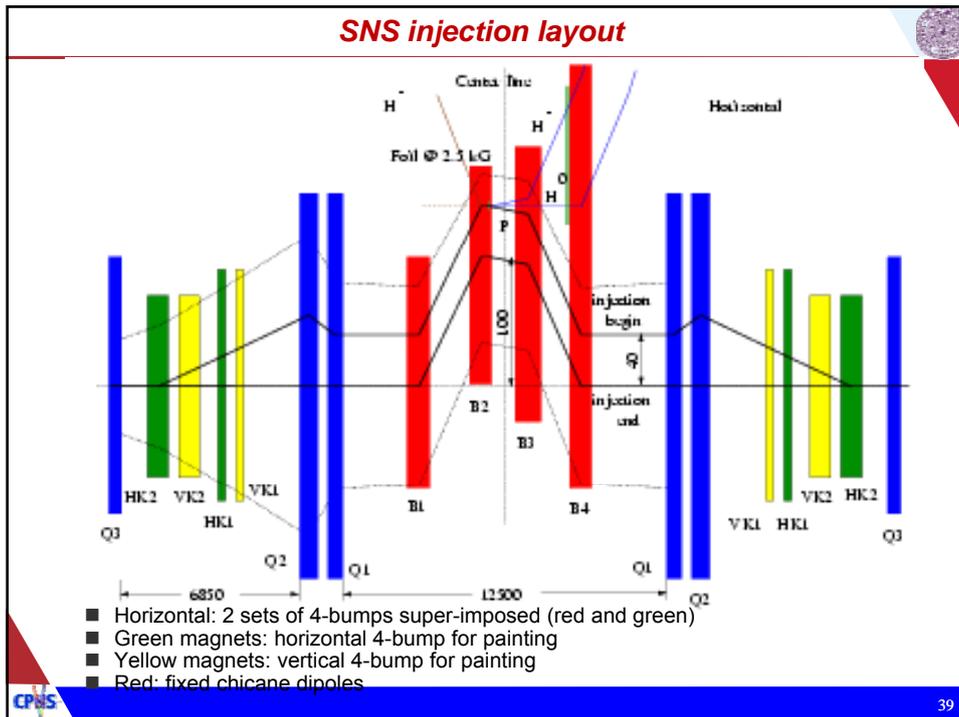
Needs a large vacuum-pipe aperture and a long straight section



## 2.3 Injection

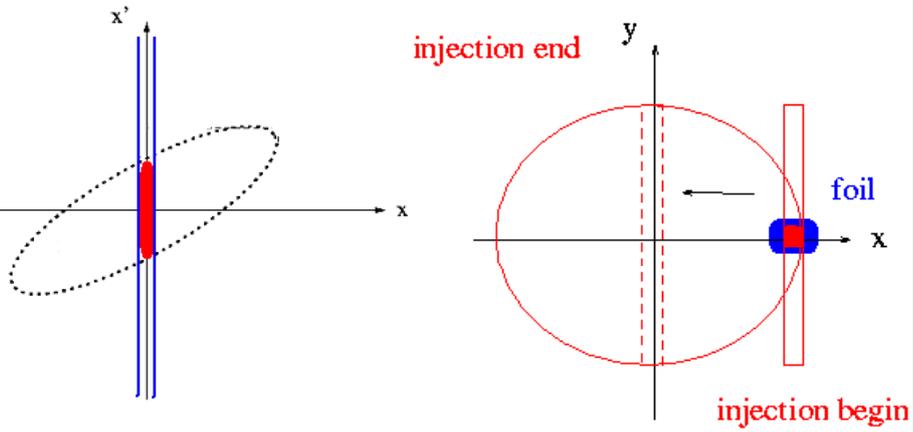
### SNS ring injection layout



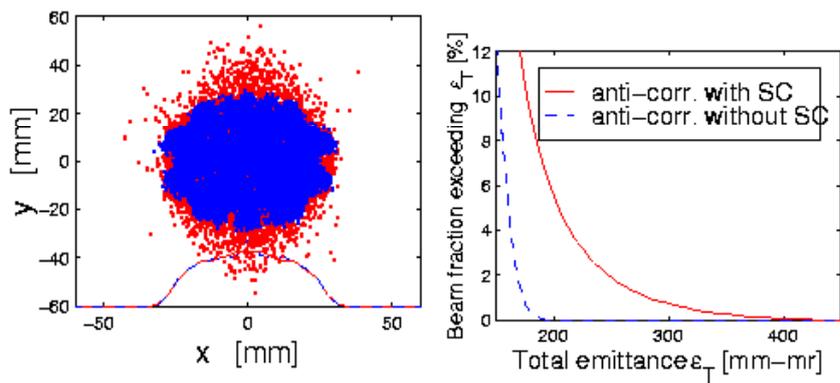


### Vertical steering/horizontal painting

- Steer in one direction, painting in the other



### Space charge & halo formation



Disadvantage of not painting over halo (vertical direction)

## Stripping of H and H<sup>0</sup>

- General loss criteria for stripping in HEBT and injection:
  - < 10<sup>-7</sup> per meter beam loss
- Gas stripping sets a limit on vacuum pressure
  - 5x10<sup>-8</sup> ~ 10<sup>-7</sup> Torr
- Electro-magnetic Lorentz stripping on H<sup>-</sup> beam
  - Mean decay length in laboratory frame

$$\lambda_s = \frac{A_{s1}}{B} \exp \frac{A_{s2}}{\beta\gamma B},$$

$$A_{s1} = (2.47 \pm 0.09) \times 10^{-6} \text{ Tm}, \text{ and } A_{s2} = 15.0 \pm 0.03 \text{ T}$$

- Less than 3 kG field for 1 GeV beam
- H<sup>0</sup> stripping
  - Require specific field (<+/-5% error) maintain decay lifetime of certain quantum state (n=5) H<sup>0</sup> from pre-mature stripping
  - Foil residing in a trailing field at 2.4 kG

## Collection of stripped electrons

PSR stripped electron burn

Injection vacuum chamber

(Courtesy W. Meng, J. Brodowski, YY Lee, D. Abell, R. Macek et al)

injection chicane #2 2:38 PM

Tapered magnet pole  
Vacuum chamber wall

Stripping foil  
Stripped proton beam

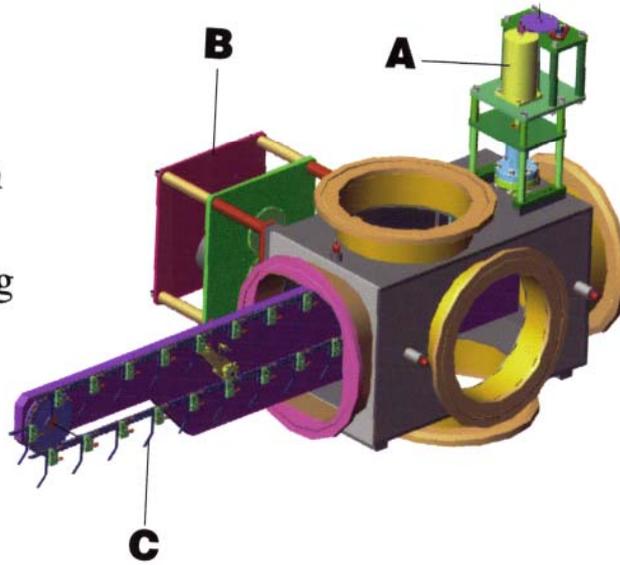
Injecting H<sup>-</sup> beam  
Stripped electrons  
Clearing electrode  
Electron collector

Water cooled copper plate

Tapered magnet to guide stripped electrons (~ 2 kW), compensated for the circulating beam  
Carbon-carbon collector on water-cooled copper plate  
Clearing electrode (~ 10 kV) to reduce scattered electrons  
Video monitors on foil & collector

*SNS injection foil device*

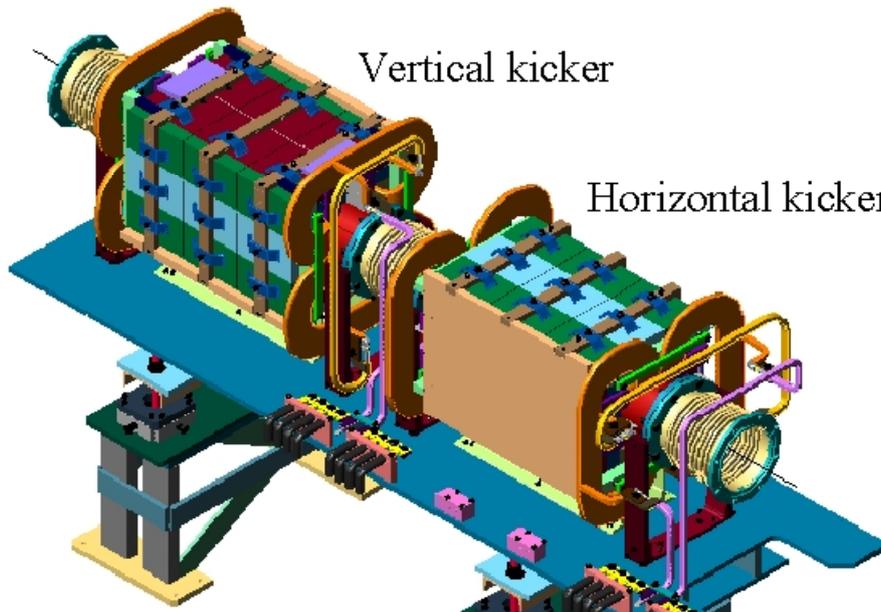
- A.** Foil Insertion Control
- B.** Foil Changing Control
- C.** Foil Holders



*SNS injection kicker*

Vertical kicker

Horizontal kicker



## Injection vacuum chamber coating

(Hseuh, He, Todd ...)

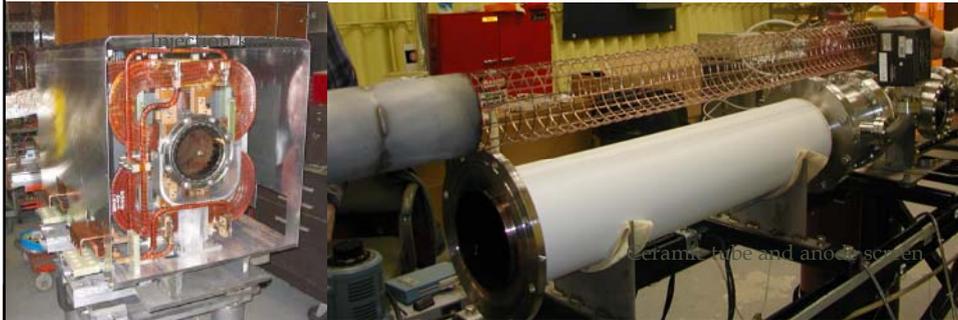
### Injection kicker ceramic chamber double coating

Cu (~ 0.7  $\mu\text{m}$ ) for image current

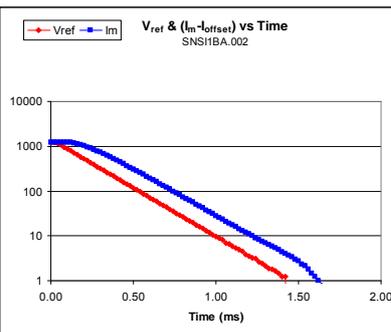
TiN (0.1  $\mu\text{m}$ ) for electron cloud

Meets requirement: conductive coatings w/ end-to-end resistance of  $\sim 0.04\Omega \pm 50\%$  (Henderson, Davino)

Thickness uniformity  $< \pm 30\%$



## Injection kicker time response measurement



Expected time constant [ms]	0.15	0.2	0.25	0.3	0.4
Measured time constant [ms]	0.171	0.213	0.260	0.307	0.402

- Satisfactory time response ( $< 0.2$  ms)
- Interference from vacuum chamber/coating not noticeable
  - 700 nm Cu and 100 nm TiN
- Need to verify magnet-to-magnet matching

### Longitudinal painting

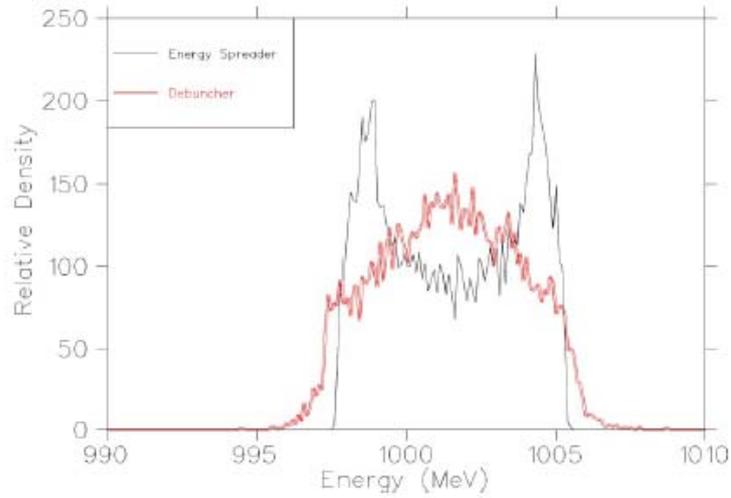


FIG. 28. (Color in online edition) Energy distribution at the injection foil, using either an energy spreader or a conventional debuncher. An energy spreader significantly suppresses the beam tail (Sec. III.C.4).

### Longitudinal painting

- “sharpen” the painting pen by reducing momentum spread before injection (correcting energy jitter, e.g.)
- Paint the momentum space by modulating the injecting beam energy

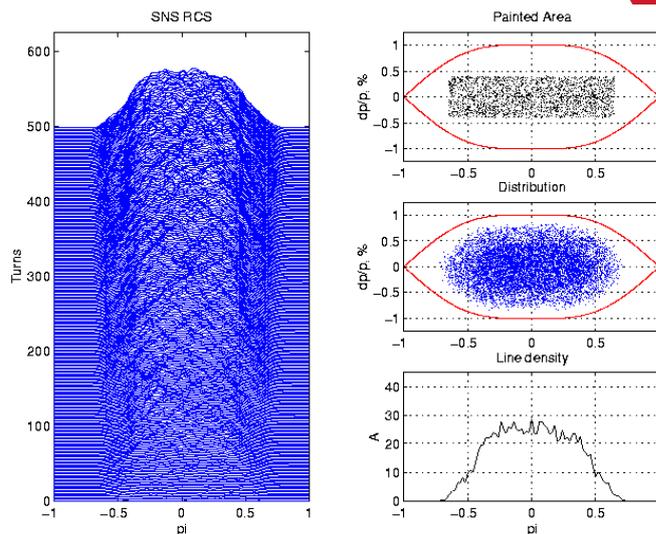
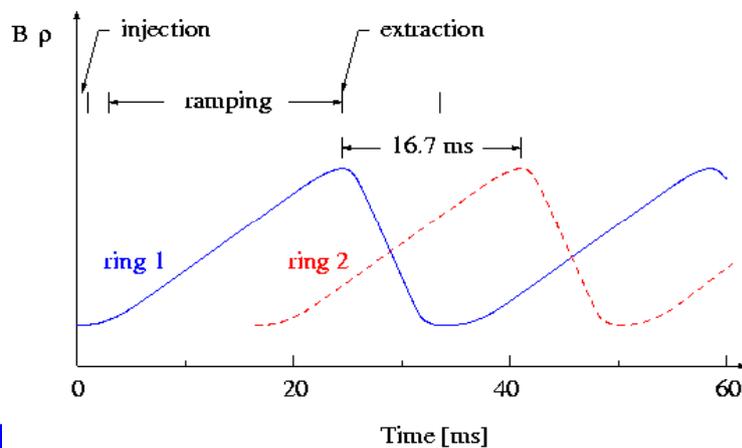


Figure 7: Longitudinal bunch evolution during injection with a dual ( $h = 2$  and  $h = 4$ ) RF system. The full injection momentum spread at the end of HEBT line is  $\Delta p/p = \pm 0.4\%$ , the peak current is 26 A, and the bunching factor is 0.46.

## 2.4 Acceleration

### *Ramping*

- Prefers injection “flat-bottom” and extraction “flat-top”
- Simplest scheme for RCS: sinusoidal resonance ramp
- Possibly slower up-ramp and faster down-ramp
- Smooth variation of longitudinal parameters



## Program of RF voltage & phase

- Beam loss often occurs at initial ramping due to reduction in bucket area when the synchronous phase is increased
- Careful program of voltage and phase to ensure monotonic increases of bucket area
- Keep the process adiabatic

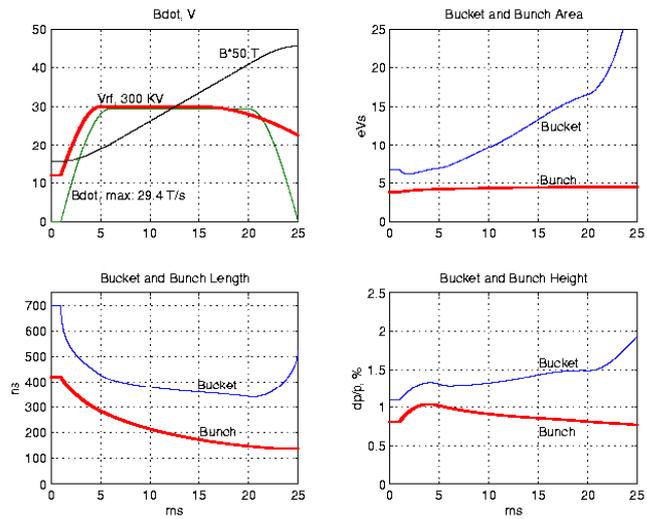


Figure 8: Programming of RF voltage and magnetic field, and the evolution of momentum spread, bunch area and bunch width in comparison with the  $(h=2)$  RF bucket.

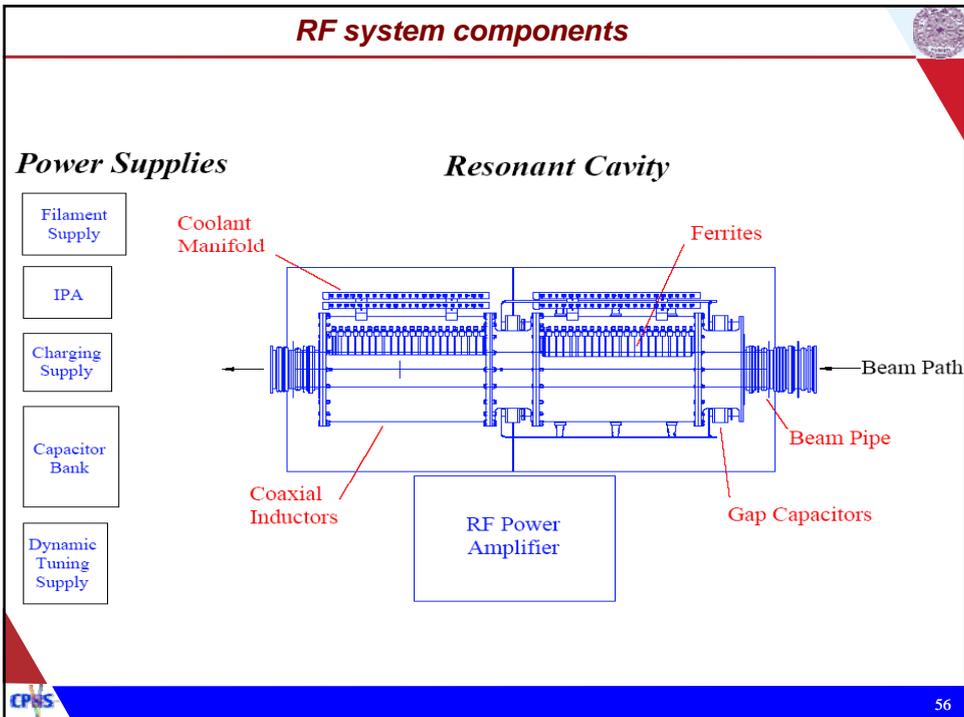
## SNS ring RF cavities



### SNS RF system at ORNL



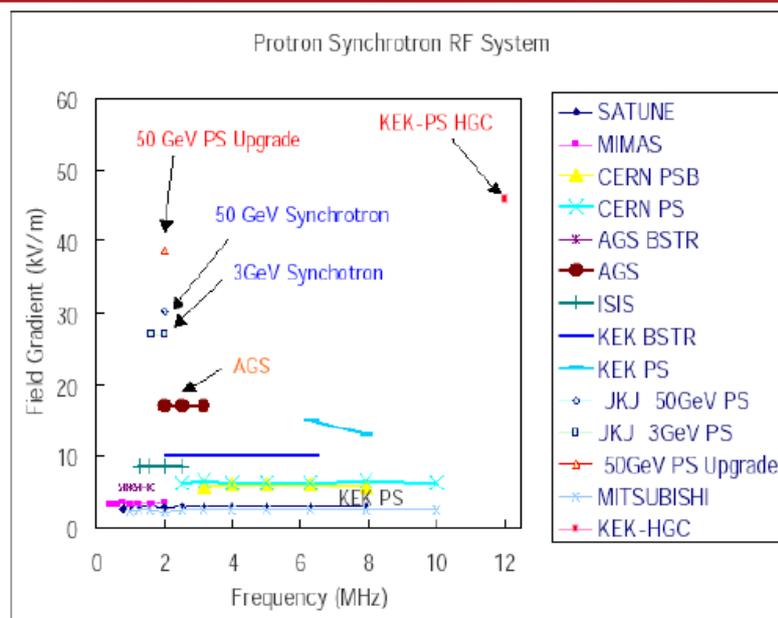
### RF system components



### Ferrite-loaded cavities

- Frequently used when variable resonance frequency is needed to follow the change of beam speed
- Cavity acts as a resonance transformer with the beam as the secondary winding
- Ferrite serves two purposes
  - Enhances the magnetic field for given current, allowing a small cavity size
  - Allow dynamic tuning of the cavity

### RF cavity gradient upgrade at J-PARC



## 2.5 Extraction

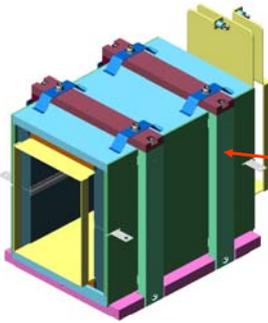
### *Extraction (single-turn)*

- Typical high-activation area
- Measures to control beam loss
  - Clean beam gap before extraction
  - Wide extraction channel, tolerable to 1 kicker failure
  - Beam position on target immune to kicker failure
- Impedance control
  - Kickers often reside inside vacuum chamber – needs to minimize coupling impedance and to perform special coating
- Maintainability
  - Remove device (pulse forming network, etc.) outside of tunnel

### SNS extraction kicker (14 units)

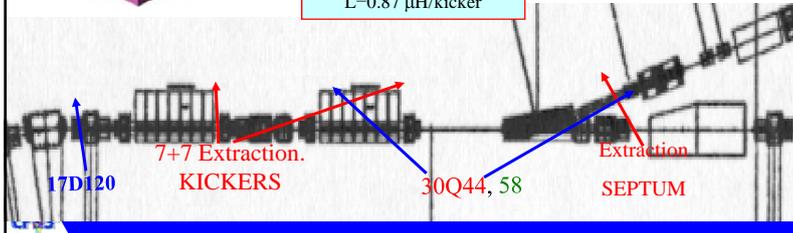
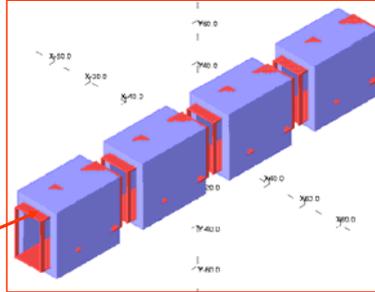
- Ferrite kicker inside vacuum pipe to allow fast field variation
- Variable gap height/width (optimize impedance, power load, clearance)

Magnet Type : WF (Ferrite)  
 Ferrite Length : 0.35 m  
 $\int Bdl$  : 9.5 to 6.5 kGauss.cm  
 Gap (Hor.) : 13.8 to 19 cm  
 Width (Vert.) : 13.1 to 24.8 cm  
 Rise time to 95% : 200 nsec  
 Maintain peak field: 750 nsec



Single kicker 3-D Calc.  
 $\int Bdl=7.0$  kGauss.cm/kicker  
 $L=0.81$   $\mu$ H/kicker

4-Kickers in Tandem  
 $\int Bdl=6.75$  kGauss.cm/kicker  
 $L=0.87$   $\mu$ H/kicker



### Extraction septum magnet

- Lambertson septum: avoids electrical elements between the circulating and extraction beam channels

Bend Angle :  $16.8^\circ$

Field Un. :  $\Delta(\int Bdl)/(B_0 L_{eff}) \leq \pm 1 \times 10^{-3}$

Iron Length : 2.44 m

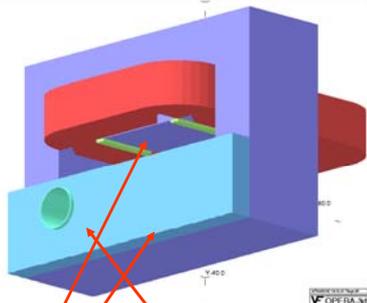
$\int Bdl$  : 1.58 Tm for 1.0 GeV

Magnet Gap :  $\sim 16.5$  cm

Septum thickness : 1 cm

Pipe ID Circ Beam : 17.5 cm

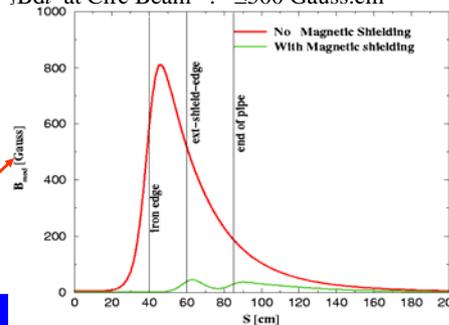
$\int Bdl$  at Circ Beam :  $\leq 500$  Gauss.cm



“Shims” of the Lambertson Septum

“Field Clam” and “Magnetic-pipe” to reduce stray fields at the circulating beam region

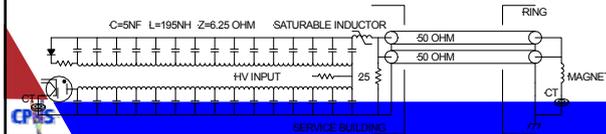
The  $B_{mod}$  of the stray fields at the center of the pipe of the circulating beam with and without “Field Clam”



### Kicker's pulse-forming network

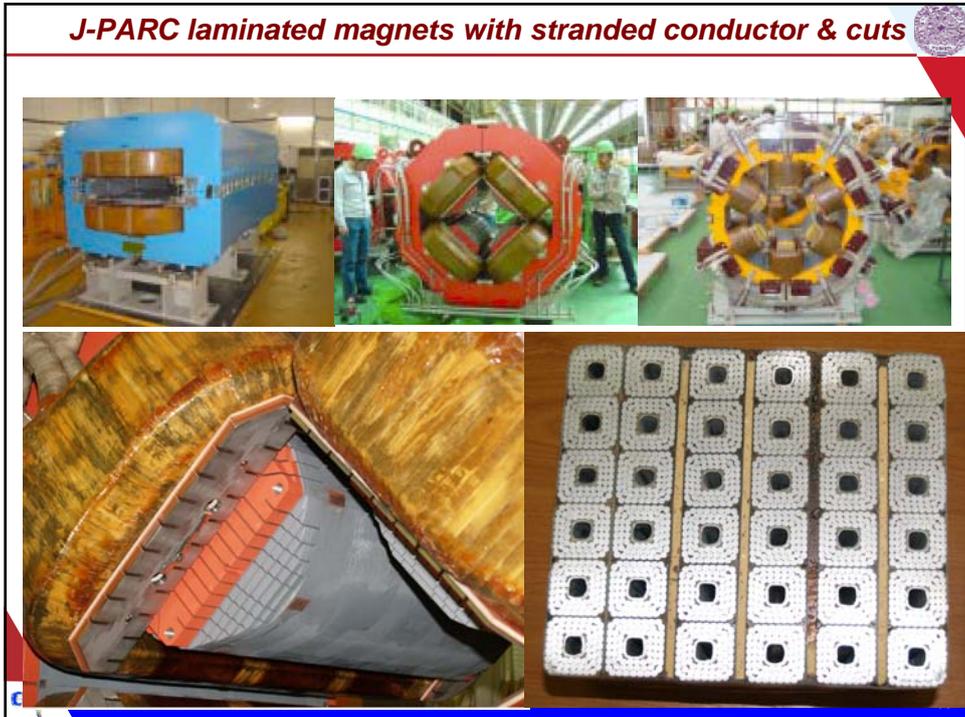


- Placed outside of the tunnel to avoid radiation damage
- Careful EMI isolation, ground break
- Optimize saturable inductor to effectively "shorten" rise time (200ns)
- Improved flat-top flatness (1%)
- PFN termination: lower impedance
- Increase magnet height to halve coupling impedance (same drive)
- Shield the terminating resistance, reducing cable reflection



63

## 2.6 Magnet system & field error compensation



## *SNS figure-8 doublet quad & rad-hard quads*



## *Magnet considerations*

- High field
  - field saturation, high current engineering
- High repetition rate
  - Eddy current, special coil (e.g. stranded coil), magnet core cuts
- Large aperture
  - Large power supply
- Close to nearby magnets
  - High magnet fringe field effects

## Typical dipole magnet

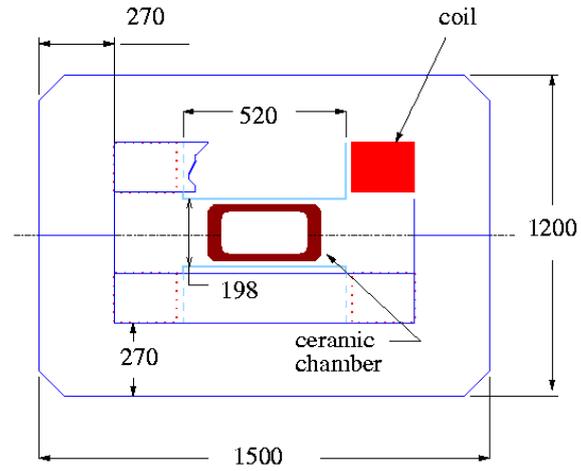
- Iron core
- Water-cooled windings
- Good field quality ( $\sim 10^{-4}$ ) achievable with iron shaping

$$N_{coil}I = gH$$

$g$  [m]: gap size,  $N_{coil}/2$ : number of turns on each pole,  $I$  [A]: current

$$B = \mu_0 N_{coil} I / g \quad [\text{T}]$$

$$\mu_0 = 4\pi 10^{-7}$$



## Magnet definitions

- 2m-pole:

dipole    quadrupole    sextupole    octupole    decapole ...



m:    1                    2                    3                    4                    5

- Normal: gap appears at the horizontal plane
- Skew: rotate around beam axis by  $\pi/2m$  angle
- Symmetry: rotating around beam axis by  $\pi/m$  angle, the field is reversed (polarity flipped)

### Magnetic multipole expansion

- 2-D multipole expansion (European convention  $m \rightarrow n+1$ )

$$B_y + iB_x = B_0 \sum_{n=0}^{\infty} (b_n + ia_n)(x + iy)^n$$

- Normalized units (reference radius, main field)

$$B_y + iB_x = 10^{-4} B_0 \sum_{n=0}^{\infty} (b'_n + ia'_n) \left( \frac{x + iy}{R_{ref}} \right)^n$$

$$2m(2k+1), \quad k = 0, 1, 2, \dots$$

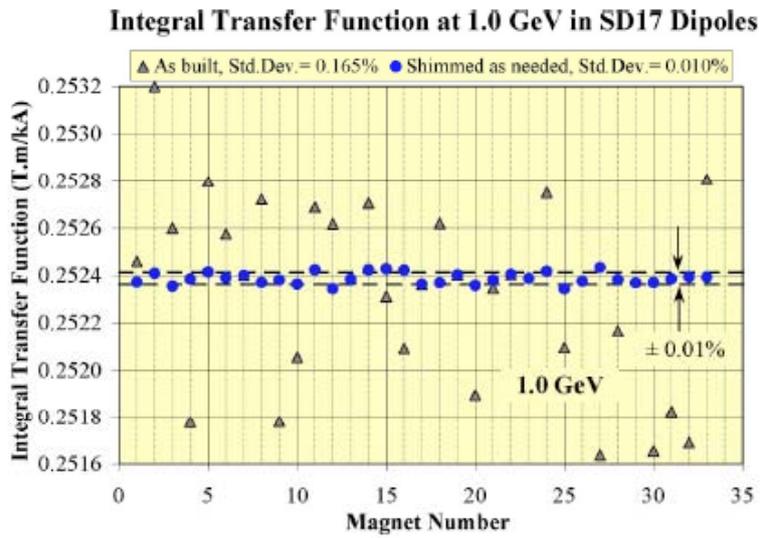
- “Allowed multipoles”: multipoles allowed by symmetry

### Measured harmonics for SNS quadrupole 21Q40

n	$a_n$	$b_n$
1	-1.4 †	-58.1 †
2	0	10000
3	-0.1	1.6
4	-0.2	1.4
5	0.0	0.1
6	0.1	1.5
7	0.0	-0.1
8	-0.1	-0.2
9	0.0	0.1
10	0.0	-0.5
11	0.0	0.0
12	0.0	-0.1
13	0.0	0.0
14	0.0	-0.1

- The boxed values are the integrated harmonics allowed by quadrupole symmetry
- All harmonics are on the required level of  $10^{-4}$  of the quadrupole field
- Remark: the large values on the dipole terms are due to errors of the measuring coil location (0.5mm centering error)

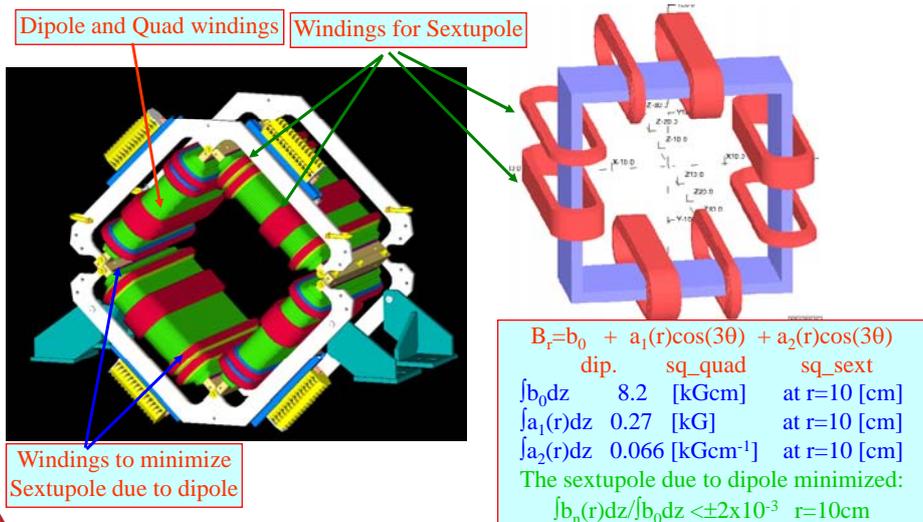
### SNS dipole integral transfer function



Shimming is optimized for 1.0 GeV operation (16X reduction in standard deviation).

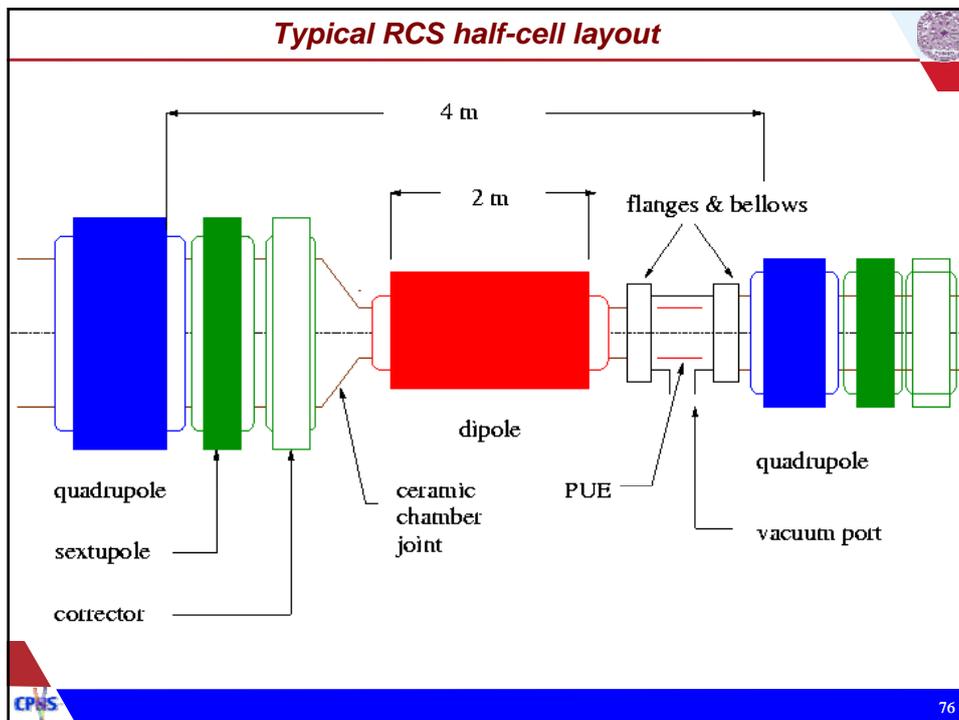
Standard deviation at 1.3 GeV operation is also reduced, but only by a factor of ~2.7.

### SNS corrector multipole 27CDM30



## 2.7 Vacuum chamber & shielding

*Typical RCS half-cell layout*



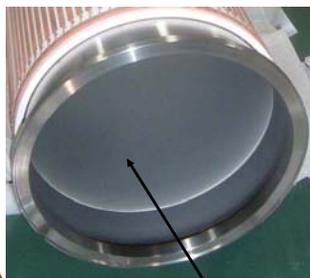
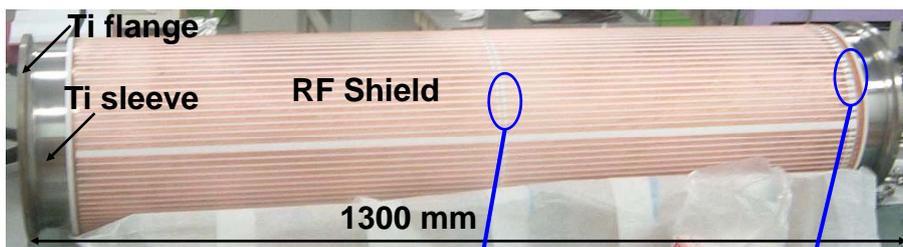
### SNS ring vacuum chamber



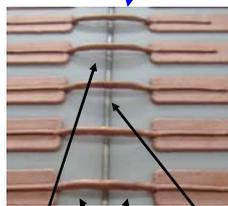
(electron detector)



### J-PARC ceramic vacuum chamber



TiN coating  
Thickness : 15 nm



Every stripes are jumped over the joint area



Capacitor  
Capacitance : 330 nF

## Vacuum considerations

- High repetition rate
  - Eddy current -> ceramic vacuum duct
- Large aperture
  - Engineering difficulties
- Beam coupling impedance
  - RF shielding of beam image current
- Electron cloud suppression
  - Surface coating of TiN

## Eddy current effects

- Eddy current induced sextupole field

$$\frac{\partial^2 B_y}{\partial x^2} = \frac{\mu_0 d_w}{\rho_r g} \dot{B}$$

- Inversely proportional to resistivity, gap height
- Proportional to ramp rate, chamber width

Leading sources of field imperfections are ramping Eddy-current and saturation. Variation in the level of saturation contributes to the tracking errors between different types of magnet. Eddy-currents induced in the vacuum chamber under the changing magnetic field distort and delay the field and generate multipole errors. For a wide chamber of thickness  $d_w$  inside a dipole magnet of gap  $g$ , the sextupole field is given by (Edwards , 1993; Rice , 1998)

## Thermal heating

Consider a pipe of thickness  $d_w$  and volume resistivity  $\rho_r$ . As an example, for a resistive loop of width  $w_r$  and height  $h_r$  penetrated by a magnetic field  $B$ , the instantaneous power per unit length is given by

$$\frac{dP_r}{ds} = \frac{B^2 w_r^2 h_r d_w}{2\rho_r} \quad (15)$$

For a circular pipe of radius  $b$ , the average power is proportional to the repetition rate, the field-variation rate, the magnetic-field amplitude squared, and the pipe's radius,  $b$ , cubed. It also is inversely proportional to the sheet-resistivity  $\rho_r/d_w$ .

## Vacuum chamber candidates

The diagram illustrates a cross-section of a vacuum chamber. A central beam path is shown with a diameter of  $260 \mu\text{m}$  and a clearance of  $520 \mu\text{m}$  plus  $5 \text{ mm}$ . The beam path is flanked by dipole poles with a gap of  $314 \text{ mm}$ . The chamber walls are labeled with dimensions: top-bottom wall  $11 \text{ mm}$ , side wall  $20 \text{ mm}$ , and a  $0.15 \text{ mm}$  metal strip. A  $4 \text{ mm}$  baking clearance is indicated. The chamber is divided into two main sections with heights of  $168 \text{ mm}$  and  $198 \text{ mm}$ . A magnetic field variation of  $\Delta p/p = \pm 2\%$  is noted. The diagram also shows a central dipole pole and a beam path.

- **Conventional:**
  - metal pipe
  - connected to magnets (FNAL Booster)
- **RCS candidates:**
  - Ceramic chamber w/ sustained shield following beam contour (ISIS)
  - Ceramic w/ printed wires (KAON study, SNS/RCS)
  - Ceramic w/ external shield & internal coating (JKJ)
  - Thin Inconel pipe (FNAL PD)

### *SNS vacuum chamber example*

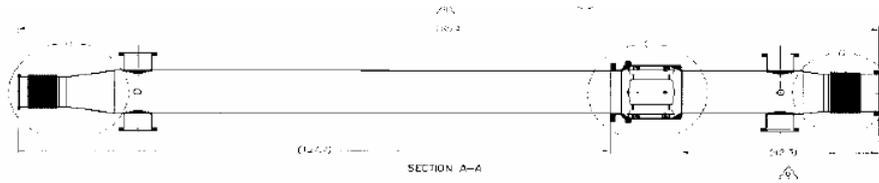
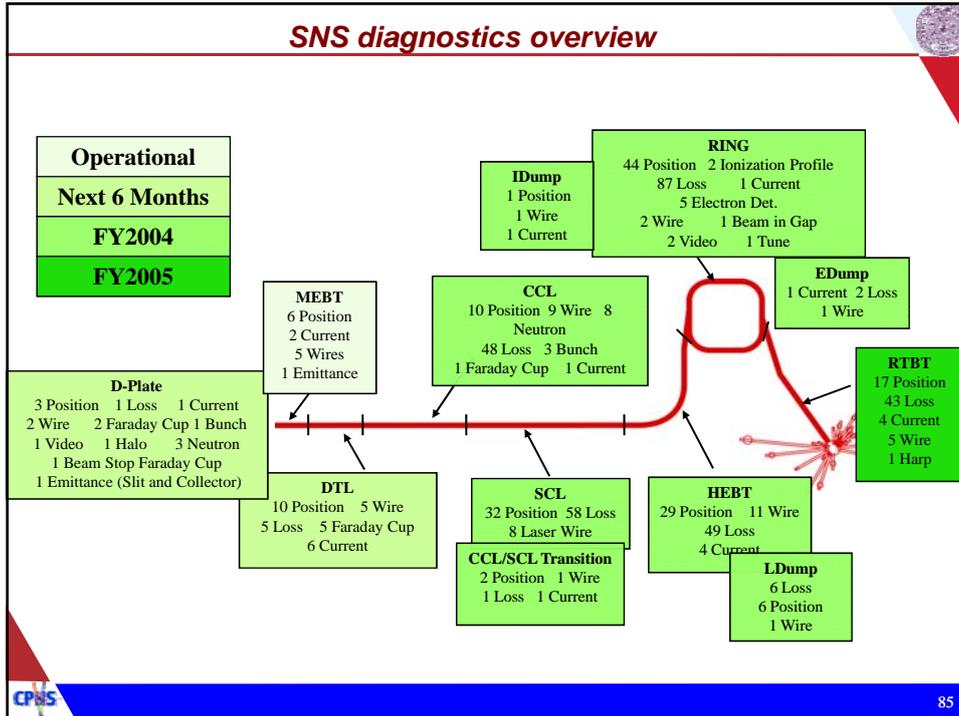


Fig. 2 Schematics of typical SNS ring straight section doublet chambers for 30cm quadrupole doublets.

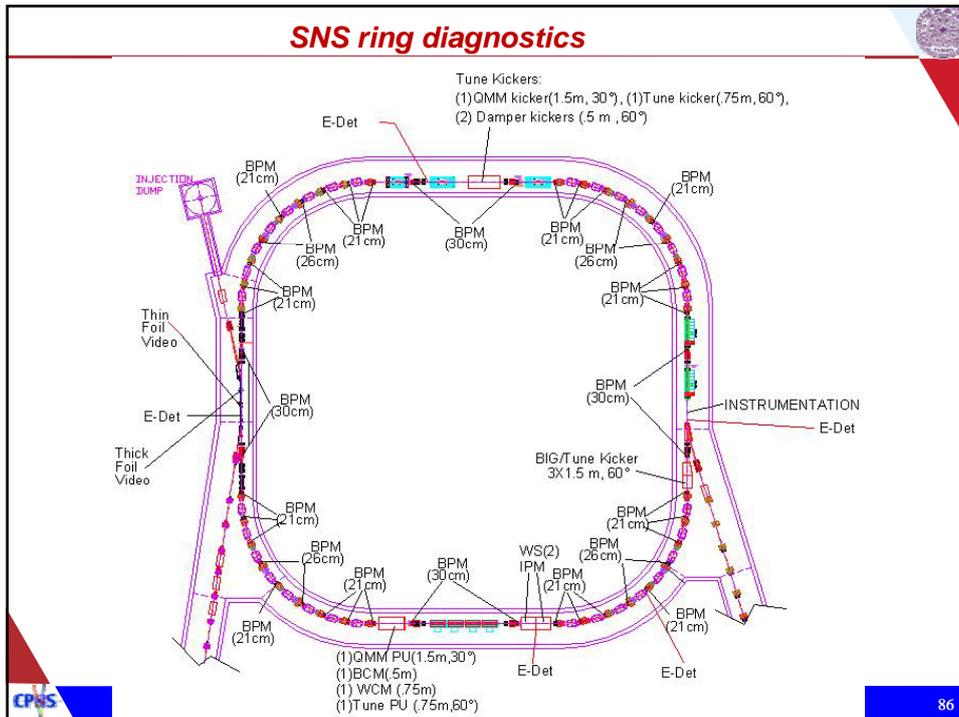
- Number of vacuum chamber type minimized
- Stainless steel pipe, inconel bellows for radiation resistance
- Inner surface coated with TiN to suppress electron cloud

## 2.8 Beam diagnostics & machine protection

### SNS diagnostics overview

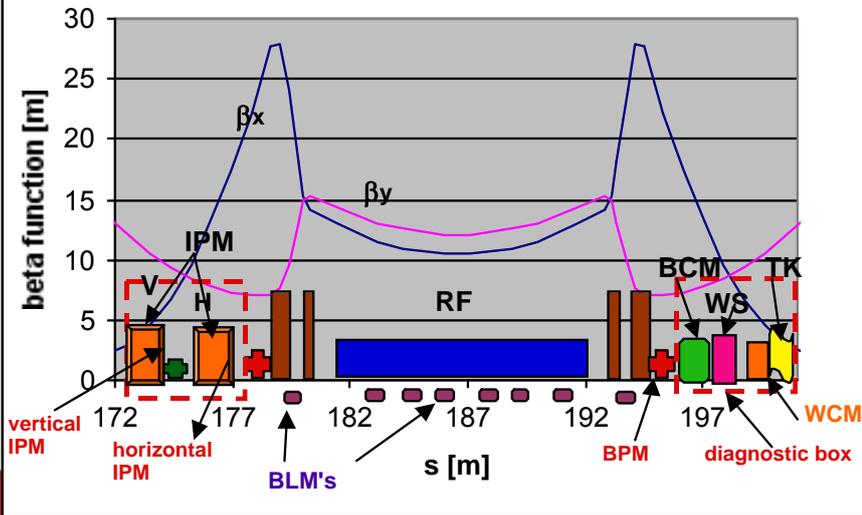


### SNS ring diagnostics



### SNS diagnostics layout example

#### Diagnostic-boxes in RF (SS) region

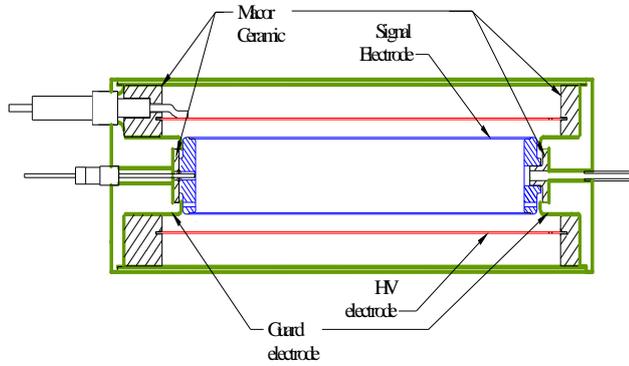


### SNS diagnostics requirements table

#### Ring System Diagnostics AP Requirements (11/2002)

Device	Location	Intensity [ppp]	Range	Accuracy	Resolution	Data structure	Comments
BPM (position)	Ring, HEBT, RTBT	5e10 - 2e14	+/- pipe radius	+/-1%	0.5/1.0%	aver./turn-by-turn	dual plane/high frequency correction for non-linear region average < 1.5e11 402.5MHz
BPM (phase)	HEBT	5e10 - 2e14	+/- 180 deg	+/-2 deg	0.1 deg		
IPM	Ring	5e10 - 2e14	+/- 64mm	2.2mm	2.2 mm	few per turn	H,V; pressure bump early
BLM (0.1 HZ)	Linac-HEBT Ring, RTBT	2e8 - 2e14	1-2.5e5 rem/h	1%	0.5 r/h	10 s averaging	1% of 1 W/m
BLM (35 kHz)	Linac-HEBT Ring, RTBT	2e10 - 2e14	1-2.5e5 rem/h	1%	50 rem/h	at 6Hz rate, sel. 10 BLMs at 10Hz	
FBLM	Linac-HEBT Ring		1-1000 rem/h			inside mini pulse intra turn	fast; not calibrated
BCM	MEBT-to-HEBT Ring-RTBT	5e10 - 2e14	15mA - 52 mA 15mA - 100A	1% 1%	.5% .5%	inside mini pulse turn-by-turn	All are Fast Current Transf.
Tune	Ring			+/- 0.001 +/- 0.005	+/- 0.0005 +/- 0.001	req. averaging req. averaging	tune kicker/pick-up - coherent BTF and QM - incoherent
Wire	HEBT Ring RTBT	5e10 - 2e11	+/- pipe radius	10%/rms width	5%/rms width	40KHz	SEM
		5e10 - 2e14	+/- pipe radius	10%/rms width	5%/rms width	40KHz	SEM+FBLM
		2e12 - 2e14	+/- pipe radius	10%/rms width	5%/rms width	40KHz	SEM+FBLM
Beam-in-gap	Ring		0 - 0.1 A	20%			BIG kicker/mon., relative acc.
Foil Video	Ring	5e10 - 2e14	Visible - near IR	+/- 1mm	+/- 1mm	standard video data	2 systems (primary, secondary), phosphor screen
e - detectors	Ring		2e8 - 2e11 (e-)	5%	1e8 (e-)	turn-by-turn	5 locations: Inj., Coll., Ext, IPM and in the arc; MCPs?
Luminescence	Ring						vacuum chambers,É

## Loss monitor detector types



Upper end loss limit: Response up to 0.5 % fast single point (Linac, HEBT), 0.1% in Ring, RTBT

Lower end loss limit: 1% resolution of 1 W/m loss over 10 sec average

- Ion Chambers
  - Main array
- Neutron Detectors
  - Photo-multipliers
  - In lower energy Linac
  - Provided by INR
- FBLMs
  - For observing sub mini-bunch losses
  - HEBT, Ring, RTBT

## Beam Current Monitors

- MEBT to HEBT 0.3 - 1000 us,
  - 15 to 52mA
  - Accuracy < 1%
  - Resolution 0.5%
  - Detail within mini-pulse

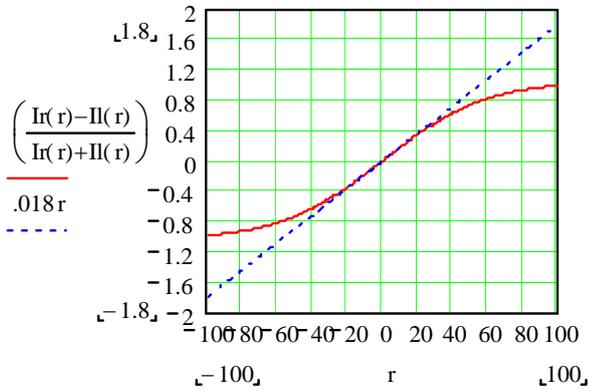
Ring to RTBT  $5e10$  to  $2e14$  Protons

- » 0.015A to 100A
- » Accuracy < 1%
- » Resolution 0.5%
- » Turn-by-turn data



LOCATION	DIAM.	NUMBER OF BCMS
Front End	5,5cm ID 13,5cm OD	2
Linac	2.5cm,3.0cm,8cm ID	DTL=6 CCL=2 SCL=1
HEBT	13cm ID	5
Ring	22cm ID	1
RTBT	22cm ID	5
TOTAL		22

## BPM processing linearity to displacement



A plot of sensitivity along the axis of a pair of pick-up elements for a 70 degree stripline designed BPM with a half aperture of 105mm. The sensitivity is shown to be 0.018 per mm. Linearity is shown to be “reasonable” over a range of +/- 20mm.

## Tune measurements

Coherent tune  
accuracy .001  
Resolution .0005  
Incoherent tune  
accuracy .005  
Resolution .0025

Hardware used: pulser, kicker, BPM & associated DAQ/processing electronics  
Initial processing executed in BPM PCI card

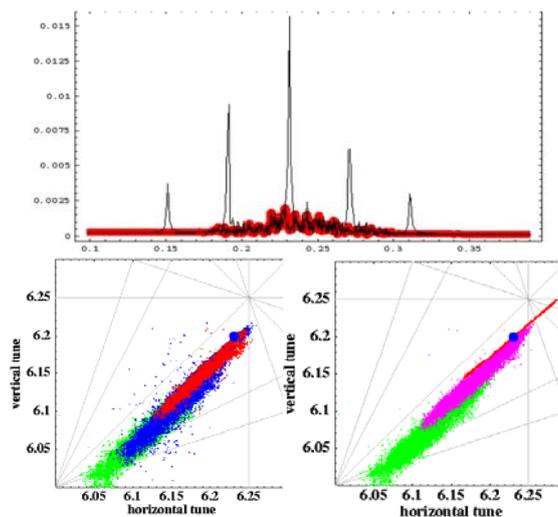
Tune calculations performed in a LabVIEW program

Measured one or more times during accumulation cycle for 1-10 turns

AP required measurement accuracy = +/- 0.001

AP required measurement resolution = +/- 0.0005

Measurement requires averaging



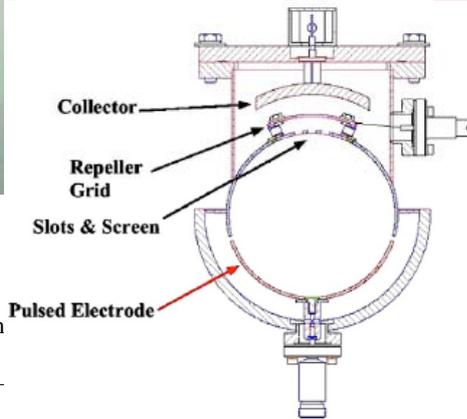
## Electron detector



Side View



Top View



Range:

100pC/cm<sup>2</sup>/turn minimum collected current  
 10nC/cm<sup>2</sup>/turn is expected to interfere with beam

We will design for the range,  $5 \times 10^{-11} \text{C/cm}^2/\text{turn}$  –  $10^{-6} \text{C/cm}^2/\text{turn}$

Data Structure:

Digitize at 400MS/s, using standard PCI scope card

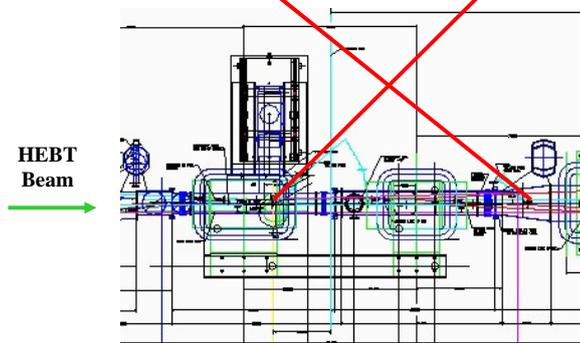


## SNS video foil monitor

Secondary (thick) Foil Camera Cubby

Primary (thin) Foil Camera Cubby

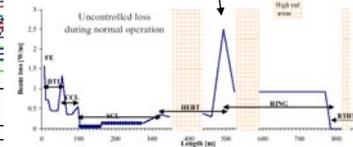
Camera to foil distance 5 meters



HEBT Beam

Paraffin or boron type neutron shield in cubbies.

Estimated Radiation levels  
 The main cause of loss at injection will be nuclear scattering at the thin carbon foil.  
 Uncontrolled loss = 2.5W/m  
 Produces about 250 R/hr at 1 ft.



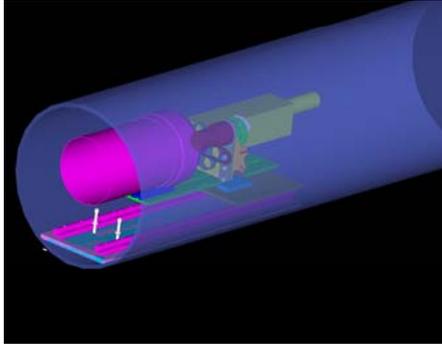
SNS/AP Tech note 7

Est. Camera Dose 10's kR/year



## SNS foil monitor video camera assembly

Dage 70RV camera, ND filter, lens assembly on rails inside cubby recessed in nearby wall.

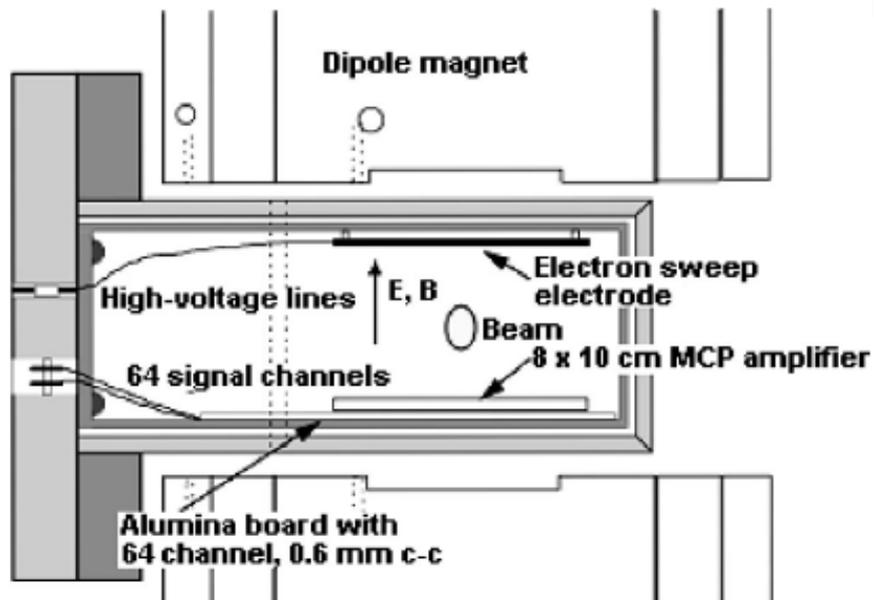


The cubby hole, camera mount, with drawer slides.



Neutral density filter assembly (C-AD):  
DC motor drive  
Geneva gear with chain  
6 positions (blank, 1, 2, 3, 4, 5)

## SNS ionization profile monitor



## SNS wall current monitor

### ■ Features

- Ferrite-loaded cavity
- Balanced gap resistors
- High current handling

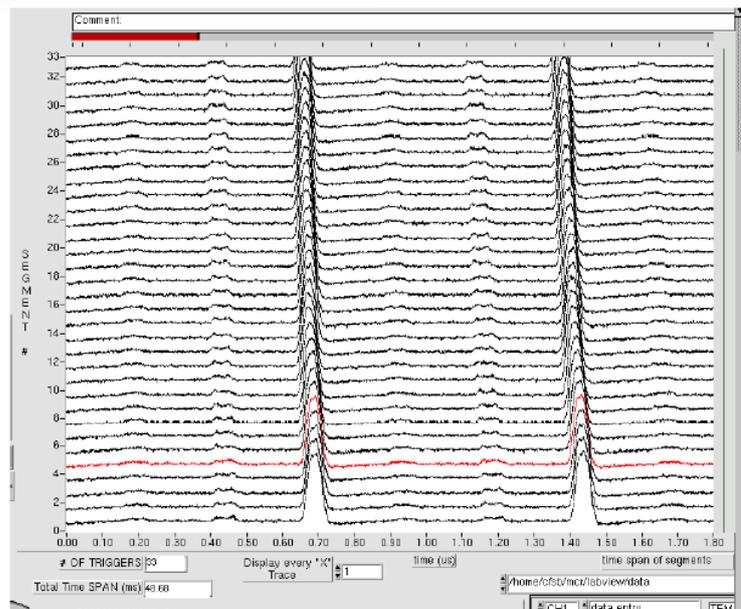
### ■ Measurements

- Beam revolution frequency
- Longitudinal profiles
- Injection phase error



## Wall current monitor profiles

Segment No.



Time (μs)

98

### 3. Beam dynamics: intensity limiting mechanisms

#### 3.1 Transverse tune shifts & resonances

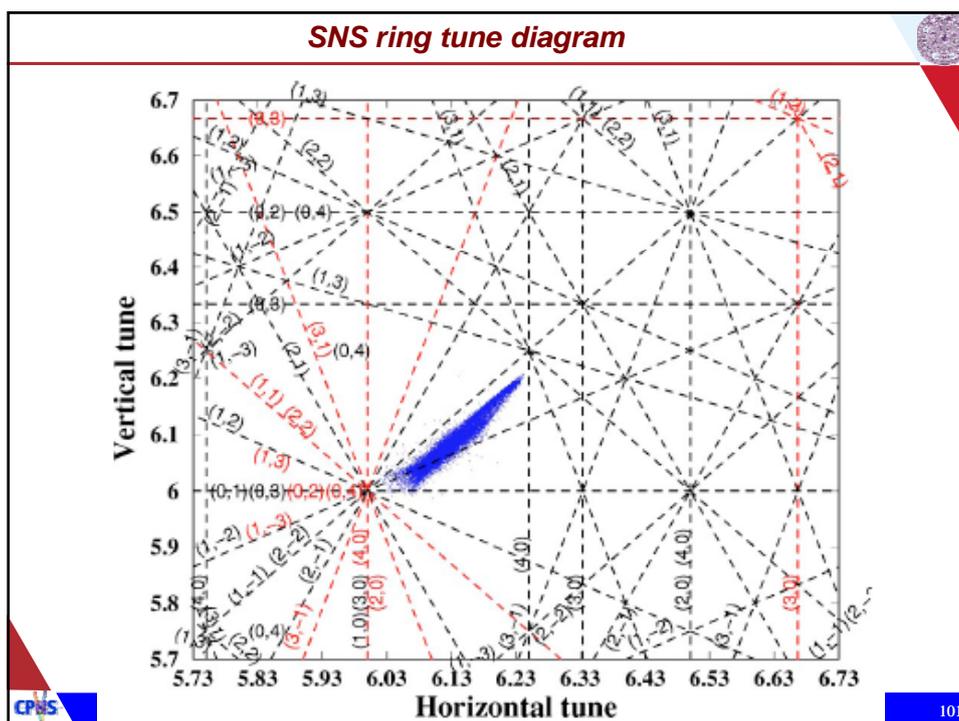


TABLE II. Tune shift produced by various mechanisms on a 2-MW beam in the SNS ring with transverse emittance of  $120\pi$   $\mu\text{m}$  in each plane and momentum spread of  $\pm 0.7\%$  (Sec. IV.A).

Mechanism	Maximum tune shift
Space charge	-0.2 (2 MW beam)
Chromaticity	$\pm 0.06$ ( $0.7\% \Delta p/p$ )
Kinematic nonlinearity ( $480\pi$ )	0.001
Fringe field ( $480\pi$ )	$\pm 0.025$
Uncompensated ring magnet error ( $480\pi$ )	$\pm 0.02$
Compensated ring magnet error ( $480\pi$ )	$\pm 0.002$
Fixed injection chicane	$\pm 0.004$
Injection painting bump	$\pm 0.001$
Electron cloud	$\sim 0.04$

## Space charge & chromatic tune shifts

■ Transverse tune shift: 
$$\Delta\nu_{sc} \approx \frac{f_{sc} N_0 r_0}{4\pi B_f \epsilon_{rms} \beta^2 \gamma^3}$$

$$\epsilon_{rms} = \sigma_{\perp}^2 / \beta_{\perp} \quad \beta_{\perp} \approx R_0 / \nu_0.$$

- Based on cancellation between electric and magnetic field for relativistic particles
- Strong dependence on energy

■ General Laslett tune shift

$$\Delta\nu_{x,y} = -\frac{f_{sc} N_0 r_0 R_0}{2\pi B_f \nu_{x,y,0} \beta^2 \gamma} \left[ \frac{1}{\sigma_{x,y}(\sigma_x + \sigma_y)} \left( \frac{1}{\gamma^2} - \eta_e \right) + A_{im}^e (\gamma^{-2} - \eta_e) + A_{im}^m \right]$$

■ Chromatic tune shift

$$\Delta\nu_{\perp} = \xi_{\perp} \frac{\Delta p}{p},$$



103

## Magnetic imperfections

$$\begin{aligned} \Delta\nu_x = & \left( -\frac{\Delta b_0}{2\rho} + \frac{b_0\delta}{2\rho} - C_1 \right) \beta_x + 3C_2\beta_x^2\epsilon_x - 6C_2\beta_x\beta_y\epsilon_y \\ & + \frac{15}{2}C_3\beta_x^3\epsilon_x^2 - 45C_3\beta_x^2\beta_y\epsilon_x\epsilon_y + \frac{45}{2}C_3\beta_x\beta_y^2\epsilon_y^2 \\ & + \frac{35}{2}C_4\beta_x^4\epsilon_x^3 - 210C_4\beta_x^3\beta_y\epsilon_x^2\epsilon_y + 315C_4\beta_x^2\beta_y^2\epsilon_x\epsilon_y^2 \\ & - 70C_4\beta_x\beta_y^3\epsilon_y^3 + \frac{315}{8}C_5\beta_x^5\epsilon_x^4 - \frac{1575}{2}C_5\beta_x^4\beta_y\epsilon_x^3\epsilon_y \\ & + \frac{4725}{2}C_5\beta_x^3\beta_y^2\epsilon_x^2\epsilon_y^2 - 1575C_5\beta_x^2\beta_y^3\epsilon_x\epsilon_y^3 \\ & + \frac{1575}{8}C_5\beta_x\beta_y^4\epsilon_y^4, \end{aligned} \quad (24)$$

$$\begin{aligned} C_1 = & \frac{1}{2}(\Delta b_1 - b_1\delta) + b_2\Delta_x - a_2\Delta_y + \frac{3}{2}(b_3\Delta_x^2 - a_3\Delta_y^2), \\ C_2 = & \frac{1}{2}\left(\frac{1}{4}b_3 + b_4\Delta_x - a_4\Delta_y\right), \\ C_3 = & \frac{1}{4}\left(\frac{1}{6}b_5 + b_6\Delta_x - a_6\Delta_y\right), \\ C_4 = & \frac{1}{8}\left(\frac{1}{8}b_7 + b_8\Delta_x - a_8\Delta_y\right), \\ C_5 = & \frac{1}{16}\left(\frac{1}{10}b_9 + b_{10}\Delta_x - a_{10}\Delta_y\right), \end{aligned} \quad (26)$$

and

$$\Delta_x = D_x \frac{\Delta p}{p} + x_c, \quad \Delta_y = D_y \frac{\Delta p}{p} + y_c. \quad (27)$$

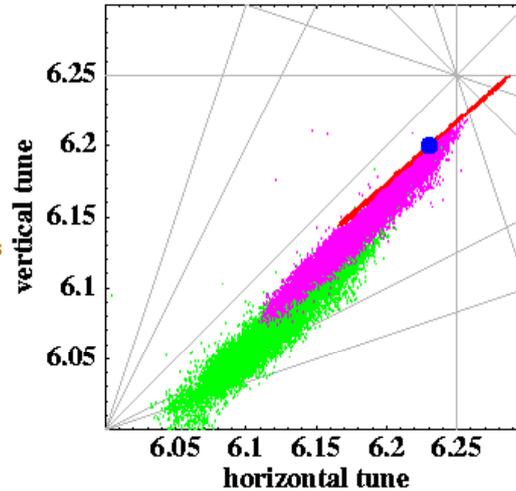
- Tune shifts and action kicks due to magnetic imperfections characterizes the impacts



104

### Combined tune spread: various intensities

w.p. (6.23,6.20) – combined tune spreads at the end of accumulation:  
 $N=0.1 \cdot 10^{14}$  - red  
 (mainly chromatic spread and resulting loss due to resonances above-chromaticity correction with sextupoles or slight w.p. adjustment)  
 $N=1 \cdot 10^{14}$  - pink  
 (depressed by space charge)  
 $N=2 \cdot 10^{14}$  - green  
 (depressed by space charge)



### Resonance condition

- Resonance condition:  $m \nu_x + n \nu_y = k$ ,  
 – resonance order  $l = |m| + |n|$ .

- Structure resonance:  $k$  is an integral multiple of the lattice periodicity

- Resonance stop band width:

$$\Delta \nu^{(m,n)} = \pm |\kappa| \epsilon_x^{|m|/2} \epsilon_y^{|n|/2} \left( \frac{m^2}{\epsilon_x} + \frac{n^2}{\epsilon_y} \right).$$

- resonance strength

$$\kappa = \frac{R_0}{\pi 2^l m! n!} \oint \beta_x^{|m|/2} \beta_y^{|n|/2} K_{\perp}^{(l)} \exp(i\Psi) d\theta, \quad K_{\perp}^{(l)} = \frac{1}{B_0 \rho} \left( \frac{\partial^{(l-1)} B_i}{\partial x^{(l-1)}} \right)$$

## 3.2 Beam loss mechanisms

### *SNS estimated controlled beam loss*

TABLE III. Estimated controlled loss of a proton beam at 1 GeV in the SNS ring, linac-to-ring transport (HEBT), and ring-to-target transport (RTBT) (Sec. IV.B.1). Losses are given as a fraction of the total beam intensity. The total beam power is 2 MW.

Mechanism	Location	Fraction	Power
<b>HEBT:</b>			
H <sup>0</sup> from linac	linac dump	10 <sup>-5</sup>	20 W
linac transverse tail	HEBT H/V collimator	10 <sup>-3</sup>	2 kW
energy jitter/spread from linac	HEBT L collimator	10 <sup>-3</sup>	2 kW
<b>Ring:</b>			
beam-in-gap	BIG kicker/collimator	10 <sup>-4</sup>	200 W
excited H <sup>0</sup> at foil	collimator	1.3×10 <sup>-5</sup>	26 W
partial ionization at foil	injection dump	10 <sup>-2</sup>	20 kW
foil miss	injection dump	10 <sup>-2</sup>	20 kW
ring beam halo	collimator	1.9×10 <sup>-3</sup>	3.8 kW
energy straggling at foil	collimator	3×10 <sup>-6</sup>	6 W
<b>RTBT:</b>			
kicker misfiring	RTBT collimator	10 <sup>-5</sup>	20 W

### SNS estimated uncontrolled beam loss

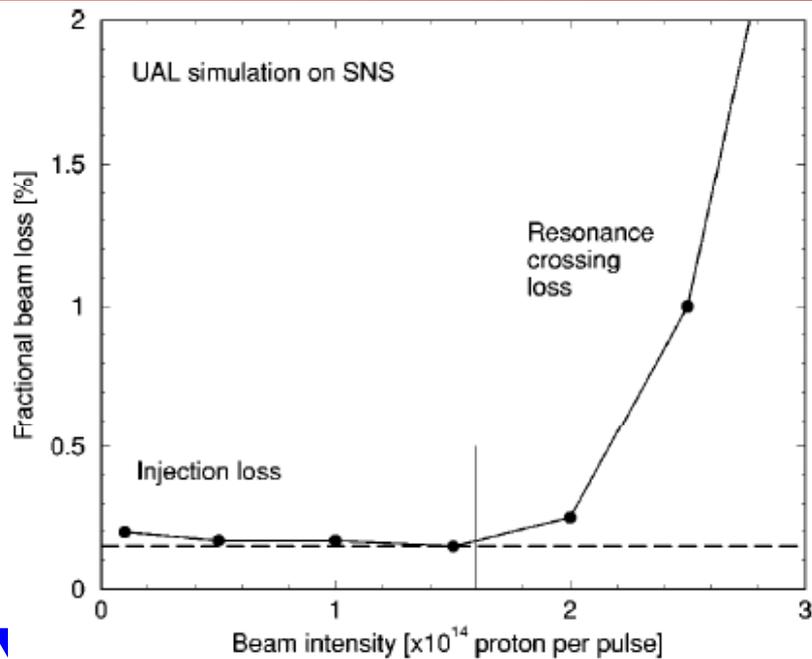
TABLE IV. Estimated uncontrolled loss of a proton beam at 1 GeV in the SNS ring, linac-to-ring transport (HEBT), and ring-to-target transport (RTBT) (Sec. IV.B.2). Losses are given as a fraction of the total beam intensity distributed in the specified machine length. The total beam power is 2 MW.

Mechanism	Location	Fraction	Length (m)	Power (W/m)
<b>HEBT:</b>				
H <sup>-</sup> magnetic stripping	all HEBT	$1.7 \times 10^{-6}$	169	0.02
collimator outscattering	HEBT achromat	$7.5 \times 10^{-6}$	15	0.1
<b>Ring:</b>				
H <sup>-</sup> magnetic stripping	injection dipole	$1.3 \times 10^{-7}$	1	0.3
nuclear scattering at foil	foil	$3.7 \times 10^{-5}$	30	2.5
collimation inefficiency	all ring	$10^{-4}$	218	0.9
<b>RTBT:</b>				
nuclear scattering at window	target window	$4 \times 10^{-2}$		



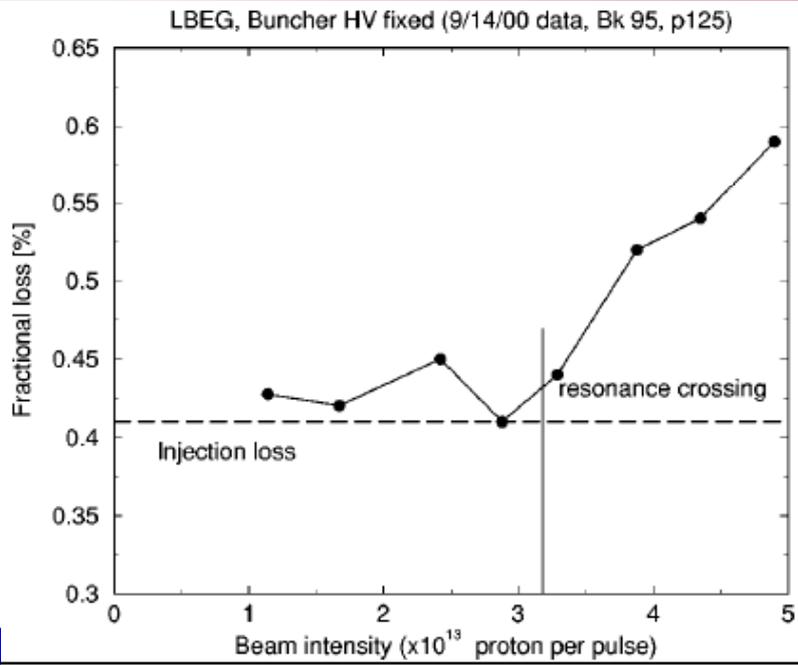
109

### Resonance loss model (SNS ring simulation)



110

### Measured uncontrolled beam loss at the PSR



### 3.3 Collective effects

## Space charge & halo formation

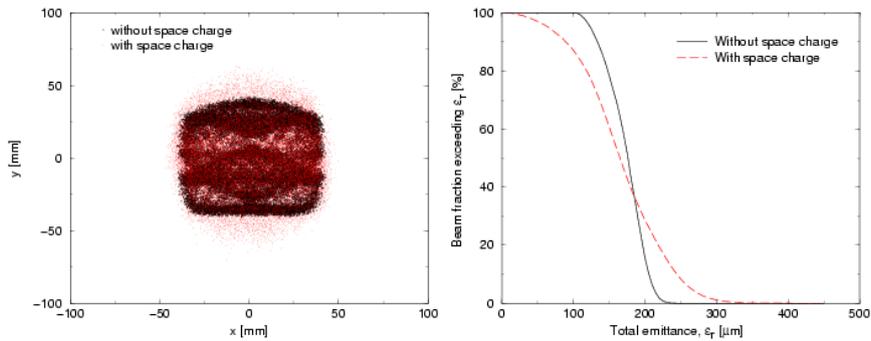


FIG. 41 Vertical emittance growth due to space charge if anti-correlated painting is used during SNS beam accumulation. The transverse tunes are (6.23, 6.20). For the data shown in black, space-charge was neglected; for the data shown in red, the space-charge force for a 2 MW beam was included. Space charge produces a significant beam tail (Section IV.C.1, courtesy A. Fedotov).



113

## Beam tail from space charge & field error

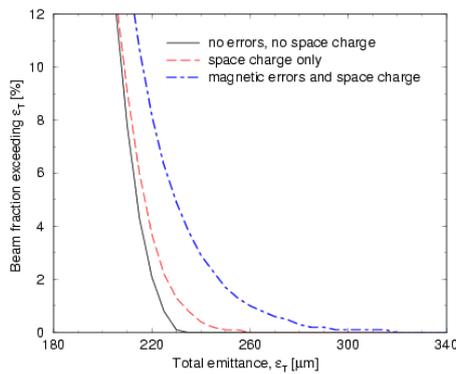


FIG. 42 Beam tail driven by space charge and magnet errors. The development of beam tail is noticeably enhanced by the combination of these two driving sources (Section IV.C.1). A non-standard working point, (6.40, 6.30), is chosen to illustrate the effect. The nominal working point, (6.23, 6.20), is chosen to avoid resonances that lead to the development of such enhanced beam tail (Section IV.C.1, courtesy A. Fedotov).



114

## Beam coupling impedance

TABLE V. Estimated beam coupling impedance of the SNS accumulator ring at frequency below 10 MHz. The beam revolution frequency is 1.058 MHz. The leading impedance source contributing to possible instability is the extraction kicker modules located inside the beam vacuum pipe (Sec. IV.C.2).

Device/Mechanism	$Z_{\parallel}/n$ ( $\Omega$ )	$Z_{\perp}$ (k $\Omega$ /m)	Comment
Space charge	$-j196$	$j(-5.8+0.45)\times 10^3$	incoherent and coherent part
Extraction kicker	$0.6n+j50$	$33+j125$	25 $\Omega$ termination at PFN
Injection kicker & pipe	$0.5/n$	17.5	pipe coated; lowest tune at 200 Hz
Injection foil assembly	$j0.05$	$j4.5$	MAFIA modeling
rf cavity	0.9 (resonance peak)	18	to be damped
Resistive wall	$(j+1)0.71$ at $\omega_0$	$(j+1)8.5$ at $\omega_0$	
Broadband beam position monitor	$j4$	$j18$	
Broadband bellows	$j1.1$	$j7$	unscreened
Broadband steps	$j1.9$	$j16$	tapered 1-to-3 ratio
Broadband ports	$j0.49$	$j4.4$	screened
Broadband valves	$j0.15$	$j1.4$	unscreened
Broadband collimator	$j0.22$	$j2.0$	

## Space charge impedances

$$Z_{\parallel}^{\text{sc}}(\omega) = -j \frac{n g_0 Z_0}{2\beta\gamma^2}; \quad Z_{\perp}^{\text{sc}}(\omega) = -j \frac{g_0 Z_0}{\beta^2\gamma^2} \left( \frac{1}{a^2} - \frac{1}{b^2} \right)$$

$$n = \omega/\omega_s, \quad Z_0 = (\epsilon_0 c)^{-1} = 377 \Omega \quad g_0 \approx 1/2 + 2 \ln(b/a)$$

- **Longitudinal**
  - Defocuses the beam longitudinally (below transition)
  - Capacitive
  - Cancellation between electric and magnetic forces results in strong energy dependence
- **Transverse**
  - Strong dependence on energy
  - Strong dependence on vacuum chamber size
  - ISIS: wire cage tapered according to beam envelope

## Resistive wall impedance

### ■ Resistive wall impedance

$$Z_{\parallel}^{\text{rw}}(n\omega_s) = n(1+j)\frac{\beta Z_0 \delta_s}{2b}; \quad Z_{\perp}^{\text{rw}}(n\omega_s) = (1+j)\frac{R_0 Z_0 \delta_s}{b^3}$$

### ■ Skin depth

$$\delta_s = \sqrt{\frac{2\rho_r}{\mu\omega}}$$

- Larger radius vacuum chamber is preferred
- Image passage through RF shielding with thickness larger than the skin depth
- Conductive coating with thickness thinner than skin depth is often used; complicated analysis

## Extraction kicker impedance iterations

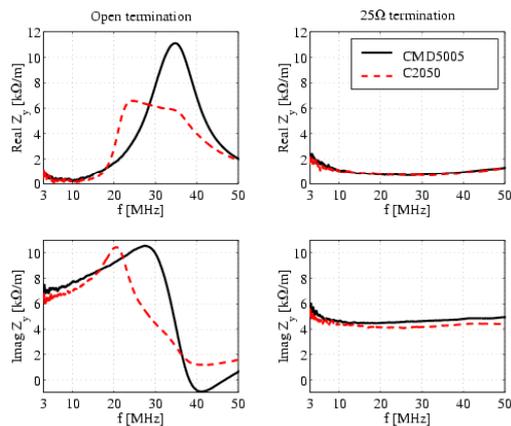


FIG. 43 Comparison of bench-measured coupling impedance for open and 25 Ω PFN termination, and high (1600) and medium (100) permeability ferrite of the SNS ring extraction-kicker assembly. The extraction kickers, residing inside the vacuum chamber of the SNS ring, are a major source of beam-coupling impedances (Section IV.C.2, courtesy D. Davino and H. Hahn).

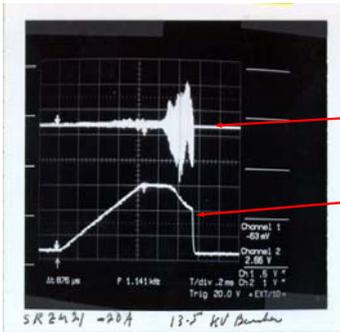
## Instabilities

TABLE VI. Collective effects and estimated thresholds for a 2-MW beam power in the SNS accumulator ring. The dominant effects are expected to be beam halo and beam loss generated by space-charge-related resonance crossing. Other intensity-limiting mechanisms include electron-cloud effects and instabilities due to the extraction kicker coupling impedance (Sec. IV.C.3).

Mechanism	Threshold	Comments
Transverse space charge	$\Delta v_{sc} \approx -0.2$	resonance crossing
Longitudinal space charge	15 kV induced RF voltage	60 kV RF voltage
Transverse microwave instability	$Z_{\perp} \approx 60 \text{ k}\Omega/\text{m}$	extraction kicker impedance
Longitudinal microwave instability	$ Z_{\parallel}/n  \approx 100 \Omega$	extraction kicker impedance
Resistive wall		(walls and kicker impedance)
( $\xi=0$ )	$Z_{\perp} \approx 1.3 \text{ k}\Omega/\text{m}$	at 200 kHz; rise time $>300 \mu\text{s}$
( $\xi=-3$ )	$Z_{\perp} \approx 100 \text{ k}\Omega/\text{m}$	at 200 kHz
Electron cloud	above 2 nC/m	above 2% neutralization in beam

## 3.4 Electron cloud effects

## Electron-cloud phenomena: PSR

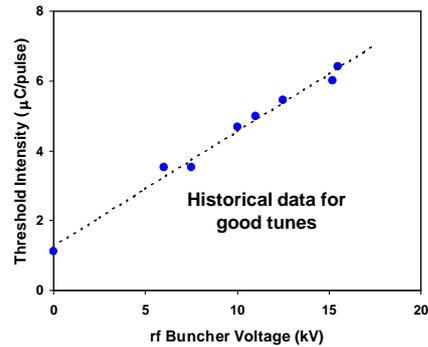


### Instability signals

BPM  $\Delta V$  signal

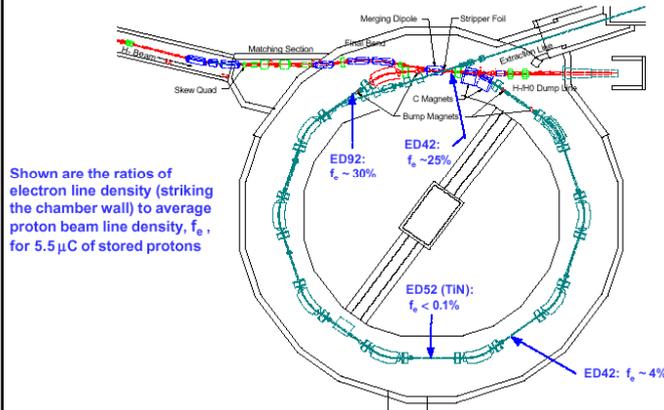
CM42 (4.2  $\mu\text{C}$ )  
(Circulating Beam Current)

### Control by rf buncher voltage



- Growth time  $\sim 75 \mu\text{s}$  or  $\sim 200$  turns
- High frequency  $\sim 70 - 200$  MHz
- Controlled primarily by rf buncher voltage
- Requires electron neutralization of  $\sim 1\%$  (from centroid model)

## Electron generation

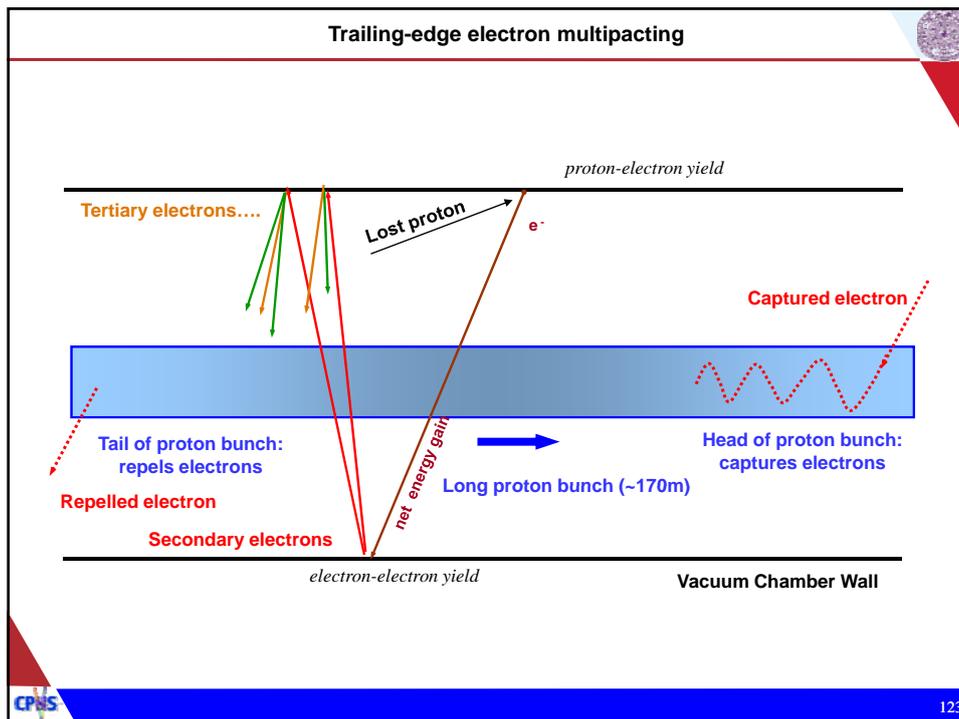


Shown are the ratios of electron line density (striking the chamber wall) to average proton beam line density,  $f_e$ , for 5.5  $\mu\text{C}$  of stored protons

### PSR e-flux measure

- High electron concentration near injection & extraction
- Electron wall-striking level to be distinguished from electron neutralization level in the bunch

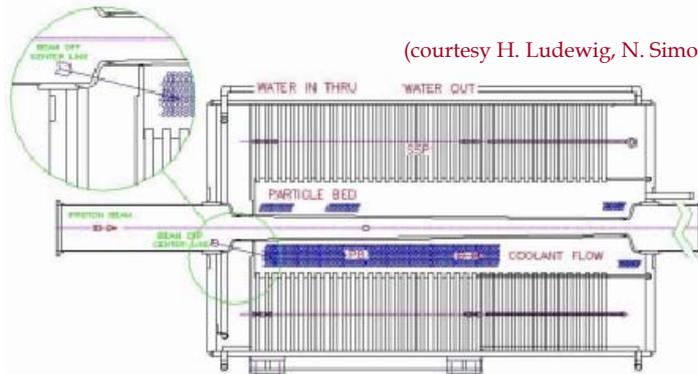
- Major sources of electrons in a high-intensity ring
  - From stripping foil ( $\text{H}^-$ ,  $\text{H}^0$ )
  - Proton striking collimators or aperture bottleneck
  - Gas ionization, ion desorption, electron desorption
  - Beam-induced electron multipacting



- ### Effects of electron clouds
- Electron neutralization, tune shifts, and resonance crossing
  - Transverse (horizontal or vertical) instability
  - Associated emittance growth and beam loss
  - Vacuum pressure rise
  - Heating & damage of vacuum chamber
  - Interferences with diagnostics system

## Electrons from collimator surface

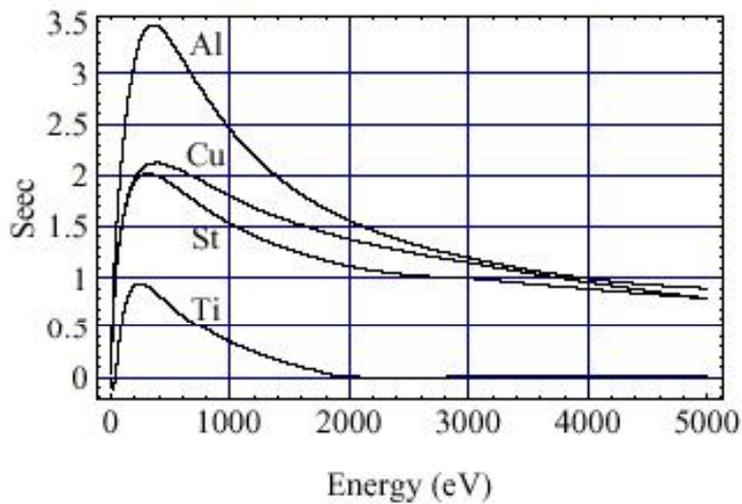
(courtesy H. Ludewig, N. Simos)



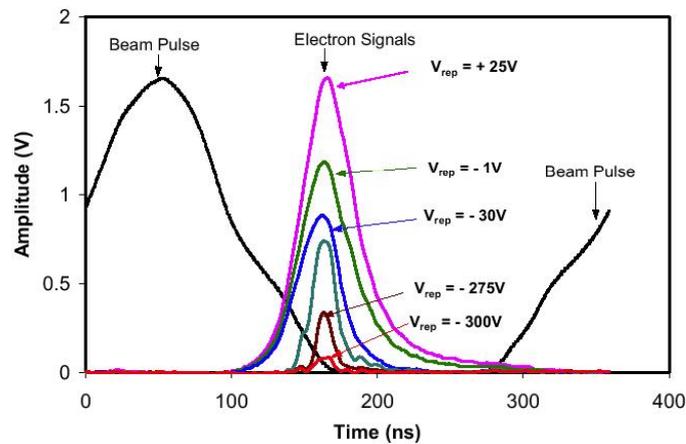
- Designed to absorb 2 – 10 kW (0.1% -- 0.5%) proton beam loss
- Beam halo at large grazing angle enhances electron production
- Possible saw-tooth surface complicated by proton stopping distance
- Possible magnetized surface proposed at LANL
- Rely on two-stage collimation for a large impact distance

## Secondary electron yield vs. primary electron energy

(courtesy N. Hilleret, O. Grobner, )



### PSR wall-electron spectrum



- Trailing-edge multipacting
- Total electrons striking the wall is  $\sim 25\%$  of the proton number
- Actual neutralization level much lower (swept electron)



127

### Preventive measures

- Suppress electron production
  - Tapered magnets for electron collection near injection foil; back-scattering prevention
  - TiN coated vacuum chamber to reduce multipacting
  - Striped coating of extraction kicker ferrite (TiN)
  - Beam-in-gap kicker to keep a clean beam gap ( $10^{-4}$ )
  - Good vacuum ( $5 \times 10^{-9}$  Torr or better)
  - ports screening, step tapering; BPMs as clearing electrodes
  - Install electron detectors around the ring
  - Two-stage collimation; winding solenoids in the straight section
- Enhance Landau damping
  - Large momentum acceptance with sextupole families; high RF voltage; momentum painting
  - Inductive inserts to compensate space charge
  - Reserve space for possible wide band damper system



128

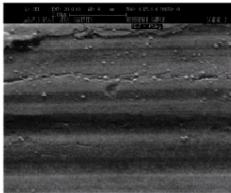
## Electron-cloud mitigation

- Inner surface of vacuum chambers coated with TiN to reduce secondary electron emission
- Solenoids used in collimation region to confine scattered electrons
- Beam-position-monitors act as clearing electrodes
- Beam-in-gap kicker to clear residuals
- Extra vacuum ports for beam scrubbing



(Courtesy H. Hseuh, P. He, M. Blaskiewicz, L. Wang, SY Zhang et al)

SEY= 2.4, as-received condition



SEY= 1.1 after air and vacuum bake

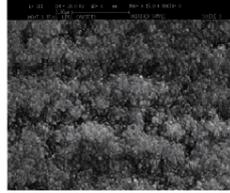
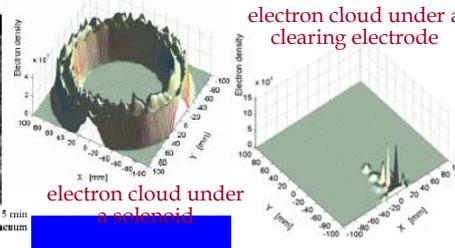


FIG. 8. Secondary electron image of copper as-received (magnification=15 000).

FIG. 9. Secondary electron image of copper after 5 min air exposure at 350 and 350 °C bakeout under vacuum (magnification=15 000).



electron cloud under a clearing electrode

electron cloud under a solenoid

## Ring vacuum chamber coating

(Hseuh, He, Todd ...)

**Injection kicker ceramic chamber double coating**

Cu (~ 0.7 μm) for image current

TiN (0.1 μm) for electron cloud

Meets requirement: conductive coatings w/ end-to-end resistance of ~0.04Ω ±

50% (Henderson, Davino)

Thickness uniformity < ± 30%

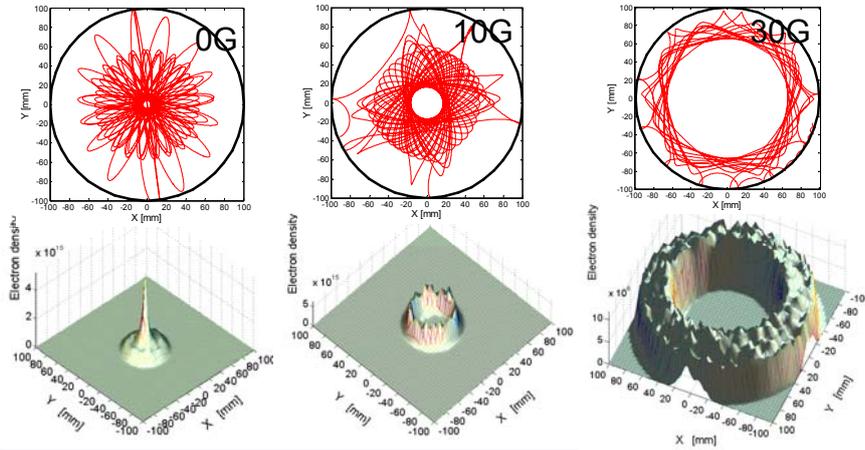
**Extraction kicker ferrite patterned TiN coating**

0.1 μm TiN on ≥ 90% inner surface, with good adhesion



**Solenoid effects (L. Wang, M. Blaskiewicz, et al)**

- **30G Solenoid field can reduce the e-cloud density with a factor 2000 !**
- **Zero density within beam**
- **Solenoid winding in the collimator straight section**



### 3.5 Computer simulation codes

## Simulation codes

TABLE VIII. Examples of beam dynamics simulation codes and their functions used for the design of high-intensity circular accelerators (Sec. IV.F). Courtesy N. Malitsky.

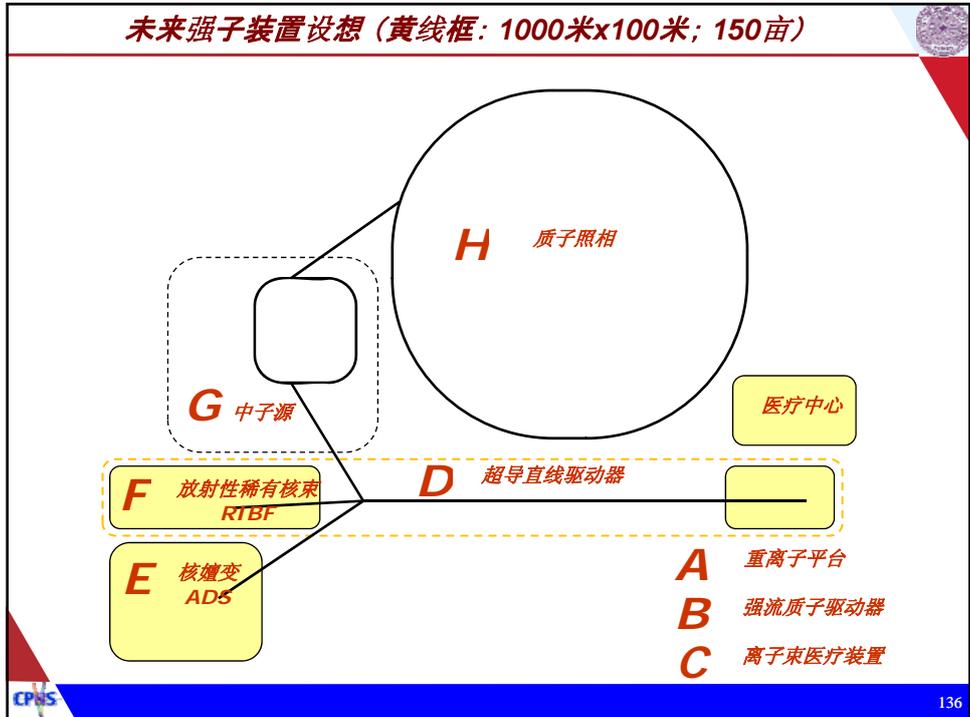
Functions	UAL	ORBIT	FTPOT	MAD	MARYLIE	ACCSIM	SIMPSONS
Interface	<b>PERL API</b>	<b>SuperCode</b>	<b>FTPOT</b>	<b>MAD</b>	<b>MARYLIE</b>	<b>ACCSIM</b>	<b>SIMPSONS</b>
MAD elements	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Errors	Yes	No	Yes	Yes	No	No	Yes
Tracking	Thin lenses	Matrices + nodes	Thin lenses	Lie algebra	Lie algebra	Matrices + nodes	Thin lenses
Mapping	Any order	Second order	Second order	Third order	Third order	Linear order	No
H Painting	Yes	Yes	No	No	No	Yes	Yes
Fringe Field	Yes (Maps)	No	No	No	Yes	No	No
Space Charge	3D	3D	No	No	No	2.5D	2D & 3D
Analysis (twiss ...)	Yes	No	Yes	Yes	Yes	No	No
Optimization (lattice ...)	No	No	No	Yes	Yes	No	No
Correction (orbit ...)	Yes	No	Yes	Yes	Some	No	No
Impedance	Yes	Yes	No	No	No	No	No
Collimator	Yes	Yes	No	No	No	Yes	No
Integration of lattices	Yes	No	No	No	No	No	No

## 4. Future applications & developments

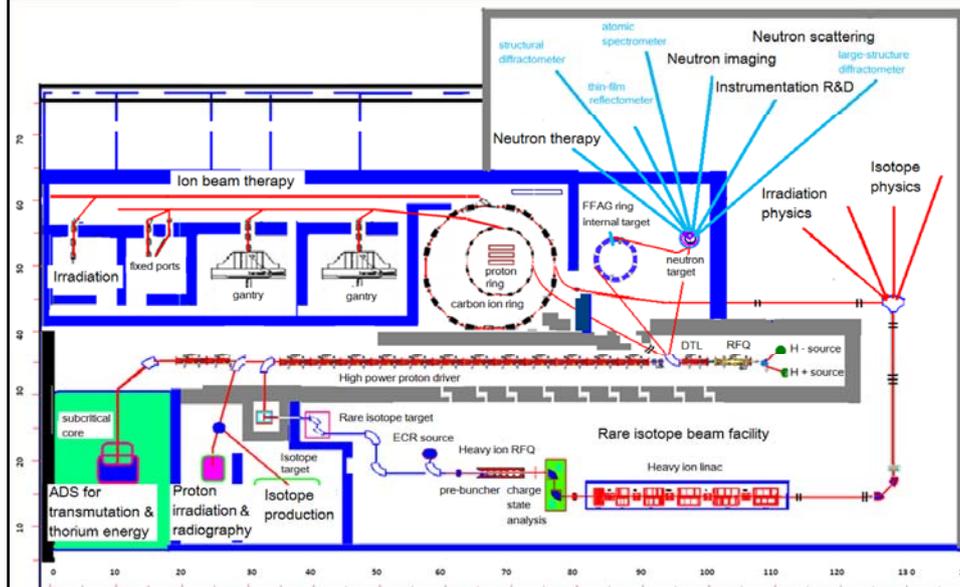
TABLE IX. Beam parameters of some existing and proposed proton accelerator facilities (Sec. V); RCS, rapid-cycling synchrotron; AR, accumulator ring; EA, energy amplifier; PD, proton driver; Linac, linear accelerator.

Machine	Intensity ( $10^{13}$ /pulse)	Rep. rate (Hz)	Flux <sup>a</sup> ( $10^{20}$ /year)	Energy (GeV)	Power (MW)	Type
Existing:						
ISIS (RAL)	2.5	50	125	0.8	0.16	RCS
AGS (BNL)	7	0.5	3.5	24	0.13	RCS
PSR (LANL)	2.5	20	50	0.8	0.064	AR
MiniBooNE (FNAL) <sup>b</sup>	0.5	7.5	3.8	8	0.05	RCS
NuMI (FNAL)	3	0.5	1.5	120	0.3	RCS
CNGS (CERN)	4.8	0.17	0.8	400	0.5	RCS
Under construction:						
SNS	14	60	840	1	1.4	AR
J-PARC 3 GeV	8	25	200	3	1	RCS
J-PARC 50 GeV	32	0.3	10	50	0.75	RCS
Proposed:						
ESS	46.8	50	2340	1.334	5	AR (2 ring)
CONCERT	234	50	12000	1.334	25	AR (2 ring)
AAA (LANL)		cw	62500	1	100	Linac
AHF (LANL)	3	0.04	0.03	50	0.003	RCS
EA (CERN)		cw	12500	1	20	Cyclotron
PD (FNAL) I	3	15	45	16	1.2	RCS
PD (FNAL) II	10	15	150	16	4	RCS
PD (BNL) I	10	2.5	25	24	1	RCS
PD (BNL) II	20	5	100	24	4	RCS
PD/SPL (CERN)	23	50	1100	2.2	4	AR (2 ring)
PD (RAL) 15 GeV	6.6	25	165	15	4	RCS (2 ring)
PD (RAL) 5 GeV	10	50	500	5	4	RCS (2 ring)

<sup>a</sup>1 year is taken to be  $10^7$  s.  
<sup>b</sup>Including planned improvements.



### *A possible layout of 10,000 m<sup>2</sup> building*



### *Class references*

- J. Wei, Reviews of Modern Physics, Vol. 75 (2003) 1383 – 1432
- 2001 US Particle Accelerator School, “Physics and design of high intensity circulator accelerators”, Colorado, USA
- 2004: US Particle Accelerator School, “The Spallation Neutron Source II: ring and transports”, Wisconsin, USA
- Handbook of Accelerator Physics and Engineering, A.W. Chao & M. Tigner

### Problem 1

- Two identical, vertically stacked rapid-cycling synchrotrons are housed in the same tunnel. The circumference is 300 m. The proton beams are injected at 400 MeV, and extracted at 2 GeV. The repetition rate is 30 Hz for each ring. The pulse in each ring contains  $10^{14}$  particles. The RF system operates at harmonic  $h=2$ , and that the pulse contains two bunches.
  - What is the total output beam power? What is the total average current of the facility?
  - What is the tolerable fractional uncontrolled beam loss in each ring?
  - What is the range of RF frequency swing?
  - The beam gap reserved for extraction kicker rise is a minimum 200 ns. Assuming that the bunch density distribution is parabolic. What is the maximum bunching factor? What is the average and peak current in the ring?



139

### Problem 2

- Let  $E$  be the total energy,  $E_k$  be the kinetic energy, and  $p$  be the momentum. Assume that the deviation in kinetic energy is much smaller than the kinetic energy. Prove that

$$\frac{\Delta E}{E} \approx \beta^2 \frac{\Delta p}{p} \qquad \frac{\Delta p}{p} \approx \frac{\gamma}{1+\gamma} \frac{\Delta E_k}{E_k}$$

where  $\beta$  and  $\gamma$  are the relativistic factors. For a proton beam of 1 GeV kinetic energy with a  $\pm 1\%$  spread in  $\Delta p/p$ , how accurate are these relations?



140

### Problem 3

- A ring consists of 4 bending arcs, each a horizontal achromat consisting of 4 identical FODO cells of  $\pi/2$  phase advance. The dispersion is suppressed. Evaluate the value and location of peak dispersion of the ring in terms of cell length, and compare it with the minimum achievable peak dispersion of a matched FODO cell.
- Repeat this exercise by flipping the polarity or the quadrupoles, i.e. DOFO instead of FODO.
- Replace the dispersion suppression method by the missing-dipole (half-field) scheme. Evaluate the minimum achievable peak dispersion in terms of cell length.
- Compare the advantage and disadvantage of the above three schemes

### Problem 4

- 1) Assume that the betatron phase advance from location  $s_1$  to  $s_2$  is  $\Delta\mu$ . Prove that the transfer matrix for  $(x, x')$  can be written as:

$$M(s_2 | s_1) = \begin{bmatrix} \sqrt{\frac{\beta_2}{\beta_1}} (\cos \Delta\mu + \alpha_1 \sin \Delta\mu) & \sqrt{\beta_1 \beta_2} \sin \Delta\mu \\ -\frac{1}{\sqrt{\beta_1 \beta_2}} [(1 + \alpha_1 \alpha_2) \sin \Delta\mu + (\alpha_2 - \alpha_1) \cos \Delta\mu] & \sqrt{\frac{\beta_1}{\beta_2}} (\cos \Delta\mu - \alpha_2 \sin \Delta\mu) \end{bmatrix}$$

- 2) Using the result of 1), prove that the condition for realizing a closed orbit bump from  $s_1$  to  $s_3$  using three dipole magnets is

$$\frac{\theta_1 \sqrt{\beta_1}}{\sin(\Delta\mu_{32})} = \frac{\theta_2 \sqrt{\beta_2}}{\sin(\Delta\mu_{13})} = \frac{\theta_3 \sqrt{\beta_3}}{\sin(\Delta\mu_{21})}$$

Here,  $\theta_i$  is the dipole kick at location  $s_i$ ,  $\Delta\mu_{ij}$  is the phase advance between  $s_i$  and  $s_j$ .

### Problem 5

- Prove that in terms of variable  $\mu(s) = \int^s \frac{ds'}{\beta(s')}$ , the normalized displacement  $X \equiv \frac{x}{\sqrt{\beta_x}}$  obeys simply harmonic motion
- With two-stage betatron betatron collimation consisting of a scraper and two collectors, prove that when the conditions
 
$$\mu_1 = \cos^{-1}\left(\frac{A}{A+H}\right) \quad \mu_2 = \pi - \mu_1$$

are satisfied, minimum number of secondary particles escape the collimation process. Here, the scraper radius A and the collector radius A+H are both defined in terms of the normalized variables

- Express the above phase-advance conditions in terms of the physical apertures



143

### Problem 6

- Consider beam density distribution in the normalized phase space during multi-turn injection. Define  $\rho^2 \equiv X^2 + X'^2$  and the quantity  $\lambda(\rho)\rho d\rho$  is the number of particle populated within the phase-space circle of radius  $\rho$  and width  $d\rho$ .
  - What is the closed-orbit function with time to realize a uniform distribution in phase space with a constant density  $\lambda(\rho)$  within a radius R during a total injection time of  $t_{\max}$  ?
  - Prove that the closed-orbit function to realize a Gaussian distribution

$$\lambda(\rho) = \frac{2N_0}{\sigma^2} \exp\left(-\frac{\rho^2}{2\sigma^2}\right)$$

is approximately

$$X_c(t) = \sqrt{2}\sigma \sqrt{-\ln\left(1 - \frac{t}{t_{\max}}\right)}$$

where the injection is performed during a time  $0 < t < t_{\max}$



144

### Problem 7

- Upon multi-turn injection of a beam with emittance  $\varepsilon_i$ , and Courant-Snyder parameters  $\beta_i$  and  $\alpha_i$ , injecting with input beam center  $(\bar{x}, \bar{x}')$  relative to instantaneous injection orbit bump. The ring beam emittance is  $\varepsilon$ , and ring Courant-Snyder parameters  $\beta$  and  $\alpha$  at injection.
  - Prove that in the normalized phase space of the ring

$$X \equiv \frac{x}{\sqrt{\beta}} \quad X' \equiv \frac{dX}{d\mu} = \frac{\alpha x + \beta x'}{\sqrt{\beta}}$$

the injecting beam ellipse becomes upright and the injection position is optimized when

$$\frac{\alpha_i}{\beta_i} = \frac{\alpha}{\beta} = -\frac{\bar{x}'}{\bar{x}}$$

the injecting beam ellipse can be described as

$$\frac{\beta_i}{\beta} X'^2 + \frac{\beta}{\beta_i} X^2 \leq \varepsilon_i$$

### Problem 7 (continue)

- Let  $X_C$  be the injection closed orbit center relative to ring beam origin in the normalized phase space of the ring. The ring emittance circle corresponding to the injecting beam ellipse can be parameterized as

$$\varepsilon(\theta) = \left( X_C + \sqrt{\frac{\beta_i}{\beta}} \varepsilon_i \cos \theta \right)^2 + \frac{\beta}{\beta_i} \varepsilon_i \sin^2 \theta$$

Assume that  $\varepsilon_i \ll \varepsilon$

show that when the condition

$$\frac{\beta_i}{\beta} \approx \left( \frac{\varepsilon_i}{\varepsilon} \right)^{1/3}$$

is satisfied, the injecting beam ellipses will all be contained by the emittance circle  $\varepsilon(\theta=0)$  (i.e. minimum phase-space dilution after injection), while the width of the injecting beam is minimum.

### *Problem 8*

- Prove that for a quadrupole magnet, the magnetic errors that are allowed by the quadrupole symmetry are quadrupole, 12-pole, 20-pole, and so on.

### *Problem 9*

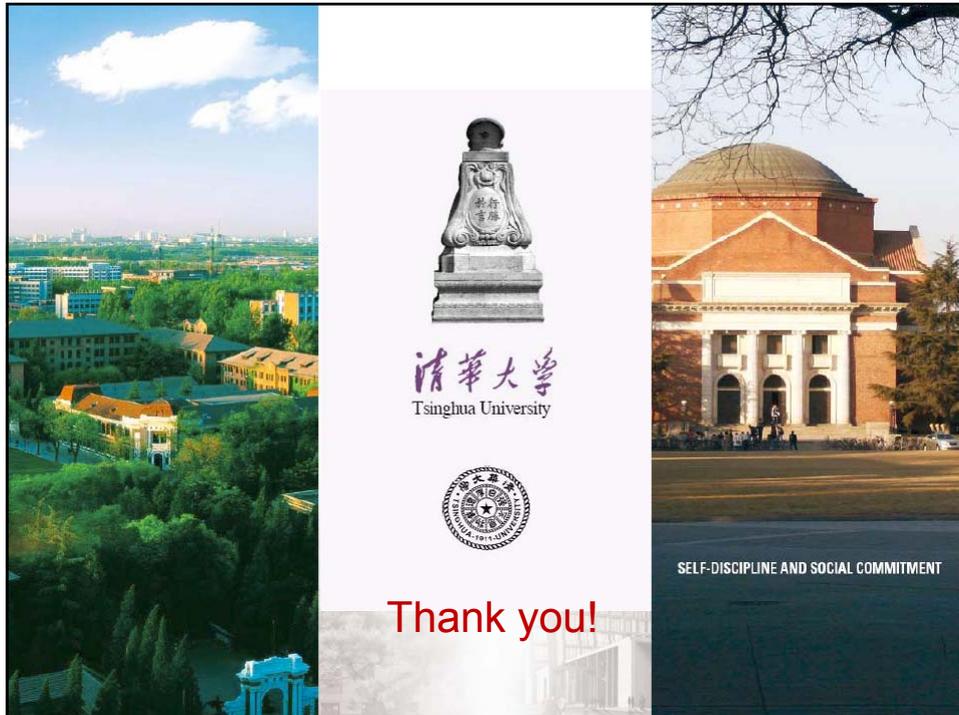
- A C-dipole magnet is designed to operate at a field of 1 T. The magnet has a width of 0.8 m, height 0.6 m. The iron material has a relative permeability of 2500. The gap height is 18 cm. The maximum current is 5000 Amp. How many turns of coil is needed for the top and bottom pole?

### Problem 10

- A  $H^-$  beam of 1 GeV kinetic energy is transported through an achromat of 90 degree bend before the ring injection. Suppose that the magnetic stripping loss criteria is for the fractional beam loss to be below  $10^{-7}$  per meter. Use the following mean decay path length (in meters in the laboratory frame)

$$\lambda_s = \frac{A_{s1}}{B} \exp \frac{A_{s2}}{\beta\gamma B}, \quad A_{s1} = (2.47 \pm 0.09) \times 10^{-6} \text{ Tm}, \text{ and } A_{s2} = 15.0 \pm 0.03 \text{ T}$$

- Estimate the maximum magnetic field that can be used to transport the beam under the loss criteria
- The achromat consists of 4 FODO cells, each containing 2 dipoles and 2 quadrupoles. What is the minimum length of the dipole?
- The beam trajectory has a maximum transverse orbit deviation of 2 cm from the magnet center in the quadrupoles. What is the maximum gradient of the quadrupole that can be used under the loss criteria?
- Estimate the maximum dipole field when the loss criteria is  $10^{-6}$  per meter instead
- Estimate the minimum dipole length when the  $H^-$  beam is injected at 8 GeV kinetic energy, and the loss criteria is  $10^{-5}$  per meter



Thank you!